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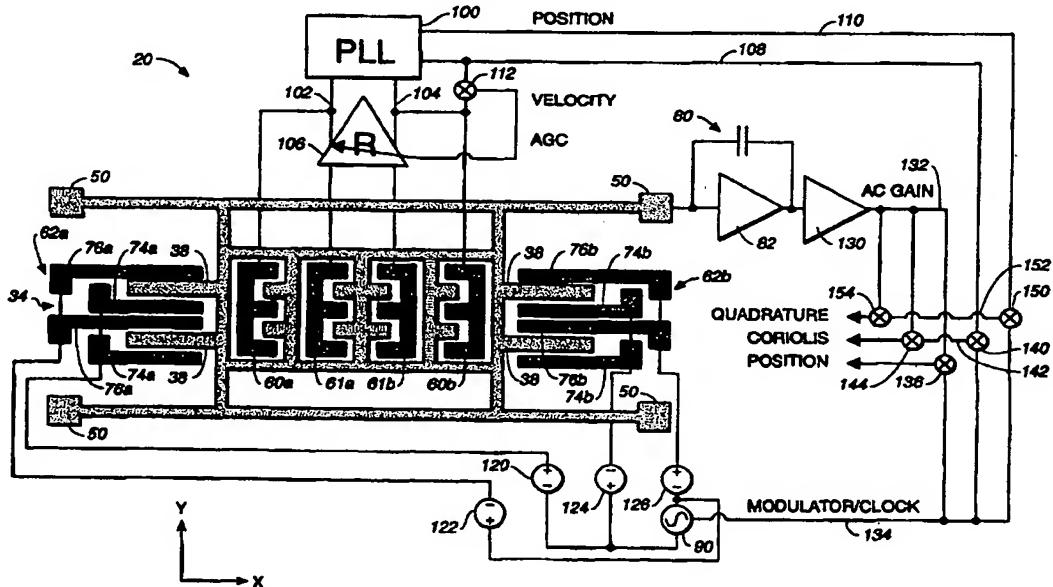
(57) Abstract

A microfabricated gyroscope to measure rotation about an axis parallel to the surface of the substrate. A voltage differential may be applied between pairs of electrode fingers to reduce the quadrature error. A microfabricated gyroscope includes a vibratory structure and interdigited electrodes having a high aspect ratio.

- 1 -

MICROMACHINED VIBRATORY RATE GYROSCOPE

Background of the Invention

5   The present invention relates generally to micro-
fabricated sensors, and more particularly to
microfabricated gyroscopic sensors.

        Multi-axis sensors are highly desirable for
inertial sensing of motion in three dimensions.
10 Previously, such sensors were constructed of relatively
large and expensive electromagnetic devices. More
recently, micromechanical sensors have been fabricated
using semiconductor processing techniques. Specifically,
micromechanical accelerometers and gyroscopes have been
15 formed from silicon wafers by using photolithographic
techniques. Such microfabricated sensors hold the
promise of large scale production and therefore low cost.

        One objective in the construction of
microfabricated sensors is to increase the sensitivity
20 and improve the signal to noise ratio of the device.
Another objective is to simplify the fabrication steps so
as to reduce the cost and complexity and to increase the
yield in the manufacturing process.

        The integration of three gyroscopic sensors to
25 measure the rotation rates about the three separate axes
coupled with three accelerometric sensors to measure the
acceleration along the three axes on a single chip would
provide a monolithic, six degree-of-freedom inertial
measurement system capable of measuring all possible
30 translations and orientations of the chip.

        It would be useful to provide a gyroscopic sensor
to measure rotation about axes parallel to the surface of

- 2 -

a substrate on which the gyroscopic sensor was
fabricated. It would also be useful to provide a
gyroscopic sensor with reduced noise.

Summary of the Invention

5   In one aspect, the invention is directed to a
gyroscopic sensor including a substrate, a mass
connected to the substrate by a suspension system, a
drive system to cause the mass to vibrate along a drive
axis substantially parallel to a surface of the
10 substrate, and a position sensor to measure a deflection
of the mass along a sense axis substantially parallel to
the surface of the substrate. Rotation of the mass about
an axis of rotation substantially perpendicular to the
surface of the substrate and vibration of the mass along
15 the drive axis generates a Coriolis force to deflect the
mass along the sense axis.

        Implementations of the invention include the
following. A processor may be coupled to an output of
the position sensor to generate a signal varying with the
20 rate of rotation of the mass about the axis of rotation.
The gyroscopic sensor may include a first sense electrode
projecting from the mass, a second sense electrode
connected to the substrate and positioned on a first side
of the first electrode, and a third sense electrode
25 connected to the substrate and positioned on an opposing
second side of the first electrode. The position sensor
may sense a change in capacitance between the first
electrode and the second and third electrodes. The
first, second and third electrodes may be substantially
30 coplanar and each electrode has a longitudinal axis
substantially aligned with the drive axis. The drive
system may include a first drive electrode projecting

from the mass, a second drive electrode connected to the substrate and positioned on a first side of the first electrode, and a third drive electrode connected to the substrate and positioned on an opposing second side of

5 the first electrode. An alternating voltage may be applied between the between the first electrode and the second and third electrodes. A voltage source may apply a voltage between a plurality of correction electrodes connected to the substrate to cause the mass to vibrate,

10 absent the Coriolis force, more precisely along the drive axis. A voltage source may apply a voltage between a first tuning electrode connected to the substrate and a second tuning electrode connected to the mass to adjust a resonant frequency of vibrations of the mass along the

15 sense axis.

In another aspect, the invention is directed to a method of sensing rotation with a gyroscopic sensor including a mass connected to a substrate by a suspension system. The mass is rotated about an axis of rotation

20 and the mass is caused to vibrate substantially along a drive axis. Rotation of the mass about the axis of rotation and vibration of the mass along the drive axis generates a Coriolis force to deflect the mass along a sense axis. A deflection of the mass along the sense

25 axis is measured, and a voltage is applied between electrode fingers connected to the substrate to cause the mass to vibrate, absent a Coriolis force, more precisely along the first axis.

In another aspect, the present invention is

30 directed to a microfabricated structure. The structure comprises a substrate, a mass connected to the substrate by a suspension system to vibrate in a plane parallel to a surface of the substrate, and three pluralities of

- 4 -

electrode fingers. The first plurality of electrode
fingers projects from the mass along a first axis in the
plane. The second and third plurality of electrode
fingers, electrically isolated from each other, are
5   coplanar with the first plurality of electrode fingers,
are connected to the substrate and project substantially
along the first axis. The first, second and third
plurality of electrode fingers are interdigitated such
that each of the first plurality of electrode fingers is
10 adjacent to one of the second plurality of electrode
fingers and one of the third plurality of electrode
fingers.

        Implementations include the following features. A
voltage source may apply a voltage between the second and
15 third plurality of electrode fingers. The structure may
further comprise a fourth plurality of electrode fingers,
coplanar with the first, second and third plurality of
electrode fingers, projecting from the mass along the
first axis, and a fifth plurality of electrode fingers
20 connected to the substrate but electrically isolated from
the second and third plurality of electrode fingers, the
fourth and fifth plurality of electrode fingers being
interdigitated. Each of the first plurality of electrode
fingers may be longer than each of the fourth plurality
25 of electrode fingers.

        In another aspect, the invention is directed to a
microfabricated structure. The structure comprises a
substrate and a suspension system to permit a mass to
vibrate in a plane parallel to a surface of the
30 substrate. The suspension system includes first and
second substantially parallel beams, each of the first
and second beams anchored at both ends to the substrate,
and third and fourth substantially parallel beams, one

- 5 -

end of each of the third and fourth beams connected to
the first beam and another end connected to the second
beam.

Implementations include the following features.
5 The structure may include a plurality of fingers
projecting along an axis substantially parallel to the
first and second beams. The structure may comprise a
fifth and a sixth beam one end of each of the fifth beam
and sixth beams connected to the third beam and another
10 end connected to the fourth beam, and a seventh beam, one
end of the seventh beam connected to the fifth beam and
another end connected to the sixth beam. The structure
may further comprise a plurality of fingers projecting
from the seventh beam along an axis substantially
15 parallel to the first and second beams. Sections of the
first and second beams located between the third and
fourth beams may be substantially rigid to prevent
rotation of the mass.

In another aspect, the invention is directed to a
20 sensor. The sensor comprises a substrate, a mass
connected to the substrate by a suspension system to
vibrate in a plane parallel to a surface of the
substrate, and three pluralities of electrode fingers.
The first plurality of electrode fingers projects from
25 the mass along a first axis in the plane. The second and
third plurality of electrode fingers, are connected to
the substrate and project substantially along the first
axis. the first, second and third plurality of electrode
fingers are interdigitated such that each of the first
30 plurality of electrode fingers is adjacent to one of the
second plurality of electrode fingers and one of the
third plurality of electrode fingers. A voltage source
applies a first DC voltage between the second and third

- 6 -

plurality of electrode fingers to cause the mass to
vibrate, absent a Coriolis force, more precisely along
the first axis.

    Implementations may include the following
 5 features. A set of electrode fingers may be positioned
opposing the three pluralities of electrode fingers, and
a second voltage source for may apply a second DC voltage
between a fifth and sixth plurality of electrode fingers
to cause the mass to vibrate, absent a Coriolis force,
10 more precisely along the first axis. The second DC
voltage may be substantially equal in magnitude but
opposite in sign to the first DC voltage. The first
plurality of electrode fingers may be electrically
coupled to the second plurality of electrode fingers.
15 The sensor may include a voltage source for applying a
third DC voltage between the first and third pluralities
of electrode fingers and the second, third, fifth and
sixth pluralities of electrode fingers to adjust the
resonant frequency of vibrations of the mass along a
20 second axis in the plane perpendicular to the first axis.

    In another aspect, the invention is directed to a
sensor. The sensor comprises a substrate, a mass
connected to the substrate by a suspension system to
vibrate in a plane parallel to a surface of the
25 substrate, and three pluralities of electrode fingers.
The first plurality of electrode fingers projects from
the mass along a first axis in the plane. The second and
third plurality of electrode fingers, are connected to
the substrate and project substantially along the first
30 axis. the first, second and third plurality of electrode
fingers are interdigitated such that each of the first
plurality of electrode fingers is adjacent to one of the
second plurality of electrode fingers and one of the

third plurality of electrode fingers. A voltage source
applies a DC voltage between the first plurality of
electrode fingers and the second and third plurality of
electrode fingers to adjust the resonant frequency of
5 vibrations of the mass along a second axis in the plane
perpendicular to the first axis.

        In another aspect, the invention is directed to a
gyroscope for sensing rotation about a Z-axis. The
gyroscope comprises a substrate, a mass connected to the
10 substrate by a suspension system to vibrate in a plane
parallel to a surface of the substrate, a drive system to
cause the mass to vibrate substantially along a first
axis in the plane, and three pluralities of electrode
fingers. The first plurality of electrode fingers
15 projects from the mass along a first axis in the plane.
The second and third plurality of electrode fingers, are
connected to the substrate and project substantially
along the first axis. The first, second and·third
plurality of electrode fingers are interdigitated such
20 that each of the first plurality of electrode fingers is
adjacent to one of the second plurality of electrode
fingers and one of the third plurality of electrode
fingers. A position sensor is coupled to the first
plurality of electrode fingers for measuring the
25 deflection of the mass along a second axis in the plane
perpendicular to the first axis. Rotation of the mass
about a Z-axis perpendicular to the surface and vibration
of the mass along the first axis generates a coriolis
force to deflect the mass along the second axis. A
30 signal processor is coupled to an output of the position
sensor to generate a signal varying with the rate of
rotation of the mass about the Z-axis.

- 8 -

Implementations include the following features. A voltage source may apply an AC voltage having a first frequency between the second and third plurality of electrode fingers. A voltage may be applied between the
5 second and third pluralities of electrode fingers to form a capacitive bridge with the first plurality of electrodes, and the position sensor may be coupled to the first plurality of electrodes to detect changes in capacitance when the mass is deflected along the second
10 axis. The sensor may includes an integrator to integrate a signal from the first plurality of electrode fingers. The drive system may generate a signal to cause the mass to oscillate along the first axis at a second frequency. The drive system may include a phase-locked loop to
15 prevent phase-shifting of the signal. The sensor may include a first mixer to mix the signal from the drive system with a signal from the voltage source. The sensor may include a second mixer to mix a signal from the first mixer with an output signal from the position sensor to
20 produce a position quadrature signal or coriolis signal. The sensor may include a mixer to mix an output signal from the position sensor with a signal from the voltage source to produce a position signal.

In another aspect, the invention is directed to a
25 microfabricated gyroscopic sensor for measuring rotation about an input axis. The gyroscopic sensor includes a substrate, a mass, and a suspension system connecting the mass to the substrate. A drive system causes the mass to oscillate substantially about a drive axis, and a
30 position sensor measures a rotation of the mass about a sense axis. Rotation of the mass about the input axis and oscillation of the mass about the drive axis generates a Coriolis force to oscillate the mass about

the sense axis. A voltage source to apply a voltage
between a plurality of electrodes associated with the
substrate to cause the mass to oscillate, in the absence
of the Coriolis force, more precisely about the drive
5 axis.

Implementations of the invention include the
following. A processor may be coupled to an output of
the position sensor to generate a signal varying with the
rate of rotation of the mass about the axis of rotation.
10 A second voltage source may apply a second voltage
between electrodes connected to the mass and the
electrodes connected to the substrate to adjust a
resonant frequency of oscillations of the mass about the
sense axis. The drive axis may be substantially
15 perpendicular to the surface of the substrate and the
axis of rotation and sense axis are substantially
parallel to a surface of the substrate. The mass may be
substantially ring-shaped. First and second pluralities
of electrode fingers may project from the mass, and third
20 and fourth pluralities of electrode fingers projecting
from the substrate and be interdigitated with the first
and second pluralities of electrode fingers. The fourth
plurality of electrode fingers may be positioned opposing
the first plurality of electrode fingers. Fifth, sixth,
25 seventh and eighth pluralities of electrode fingers may
be similarly disposed, and the pluralities of electrode
fingers are substantially co-planar. The voltage source
may apply a first DC voltage between the third plurality
and the fourth plurality of electrode fingers and second
30 DC voltage, which is substantially equal in magnitude and
opposite in sign, between the seventh plurality and the
eighth plurality of electrode fingers.

- 10 -

In another aspect, the invention is directed to a method of sensing rotation with a gyroscopic sensor including a mass connected to a substrate by a suspension system. The method includes rotating the mass about an
5   input axis and causing the mass to oscillate substantially about a drive axis. The rotation of the mass about the input axis and the oscillation of the mass about the drive axis generates a Coriolis force to oscillate the mass about a sense axis. An oscillation of
10 the mass about the sense axis is measured, a voltage is applied between electrodes associated with the substrate to cause the mass to oscillate, in the absence of a Coriolis force, more precisely about the drive axis.

In another aspect, the invention is directed to a
15 microfabricated gyroscopic sensor. The gyroscopic sensor includes a substrate having a first plurality of electrode teeth, a vibratory structure including a second plurality of electrode teeth and a suspension system connecting the second plurality of electrode teeth to the
20 substrate, the second plurality of electrode teeth interdigited with the first plurality of electrode teeth, a drive system to cause the vibratory structure to oscillate relative to the substrate, and a position sensor to measure a deflection of the mass caused by a
25 Coriolis force. The first and second pluralities of electrode teeth have thicknesses substantially greater than their widths.

Implementations of the invention include the following. The suspension system may include a plurality
30 of flexures having an aspect ratio of at least about 10:1. The first and second pluralities of electrode teeth may have an aspect ratio of at least 5:1 and may be separated by gaps having an aspect ratio of at least

10:1.

In another aspect, the invention is directed to a method of fabricating a gyroscopic sensor. An insulative layer is formed on a first substrate, a recess is formed

5   in a first surface of a second substrate, and the first surface of the second substrate is bonded to the first substrate so that the recess defines an enclosed cavity between the first and second substrates. Circuitry for the gyroscopic sensor is formed on a second surface of

10 the second substrate, and a plurality of trenches are etched in the second substrate from the second surface to the cavity, the plurality of trenches defining a vibratory structure connected to the first substrate.

Implementations of the invention include the

15 following. The vibratory structure may have a thickness of at least 25 microns and the recess may have a depth of about 1 micron. The etching step may comprise a deep reactive ion etch.

Advantages of the invention include the following.

20 The gyroscopic sensor measures rotation about an axis parallel to the surface of the substrate. The gyroscopic sensor has reduced quadrature error. The gyroscopic sensor may include a vibratory structure and interdigited electrodes with a high aspect ratio. The gyroscopic

25 sensor has a significantly reduced noise level.

Other advantages and features of the invention will be apparent from the description which follows, including the drawings and claims.

- 12 -

Brief Description of the Drawings

FIG. 1 is an schematic illustration of a spring-mass system which is equivalent to an electrostatic gyroscope.

5   FIG. 2 is a schematic perspective view of a microfabricated gyroscopic sensor according to the present invention.

FIG. 3 is a schematic top view of the movable elements of the gyroscopic sensor of FIG. 2.

10   FIG. 4 is a schematic top view of the fixed elements of the gyroscopic sensor of FIG. 2.

FIG. 5 is a schematic top view of the drive system of the gyroscopic sensor of FIG. 2.

FIG. 6 is a schematic top view of the sensing
15 system of the gyroscopic sensor of FIG. 2.

FIGS. 7A-7C are schematic illustrations of the motion of the proof mass under the influence of the Coriolis acceleration and quadrature error.

FIG. 8A is a schematic circuit diagram of an
20 integrator used to measure the position of the proof mass in the gyroscopic sensor of FIG. 2.

FIG. 8B is a schematic circuit diagram in which the integrator of FIG. 8A is replaced by a voltage buffer.

25   FIG. 8C is a schematic circuit diagram in which the integrator of FIG. 8A uses a subthreshold metal oxide semiconductor field effect transistor.

FIG. 9 is a schematic illustration of the signal processing circuitry of a gyroscopic sensor according to
30 the present invention.

FIG. 10 is a photograph of a fabricated gyroscopic sensor.

- 13 -

FIG. 11 is a graph illustrating the response of the gyroscopic sensor to rotation about the Z-axis.

FIG. 12 is a graph illustrating the response of the Y-axis resonant frequency to an applied bias voltage.

FIG. 13 is a graph illustrating the response of the quadrature error to an applied voltage differential.

FIG. 14 is a schematic top view of a gyroscopic sensor in which the sensing, driving and quadrature correcting functions are performed by different electrode structures.

FIG. 15 is a schematic of the circuitry of the gyroscopic sensor of FIG. 14.

FIG. 16 is a schematic illustration of a spring-mass system which is equivalent to a dual-axis electrostatic gyroscope.

FIG. 17A is a schematic top view of a dual-axis gyroscopic sensor according to the present invention.

FIG. 17B is a photograph of a fabricated dual-axis gyroscopic sensor.

FIG. 18 is a schematic illustration of the electronic circuitry of the dual-axis gyroscopic sensor of FIG. 17A.

FIG. 19 is a cross-sectional view along line 19-19 of FIG. 17A schematically illustrating the field lines generated by the quadrature correction electrodes.

FIG. 20 is a schematic top view of a dual-axis gyroscopic sensor in which the quadrature correction system includes electrode plates.

FIG. 21 is a schematic illustration of the circuitry of a gyroscopic sensor in which the sensing, driving and quadrature functions are combined in a single electrode structure.

- 14 -

FIG. 22 is a schematic perspective view of a gyroscopic sensor fabricated with a high-aspect-ratio vibratory structure.

FIG. 23 is a schematic circuit diagram of the
5 signal processing circuitry of the gyroscopic sensor of FIG. 22.

FIGS. 24A-24G are schematic cross-sectional views illustrating steps in the fabrication of the gyroscopic sensor of FIG. 22.

10   Description of the Preferred Embodiments
Referring to FIG. 1, a Z-axis vibratory rate gyroscope functions by generating and sensing Coriolis acceleration. The functional operation of the Z-axis vibratory rate gyroscope of the present invention is
15 illustrated by an equivalent spring-mass system. In a vibratory rate gyroscope 10, a proof mass 12 is supported by a flexible suspension 14 from a rigid frame 16. Proof mass 12 is oscillated along the X-axis (the drive mode) by a drive force F_D as the frame rotates about the Z-axis.
20 The combination of rotation and oscillation generates a Coriolis force F_c along the Y-axis on the oscillating proof mass. The Coriolis acceleration is detected as a deflection of the proof mass along the Y-axis (the sense mode).
25   Referring to FIG. 2, a micromachined gyroscopic sensor 20 designed according to the present invention includes microelectromechanical sense element or proof mass 22 connected to a rigid frame or substrate 24. The gyroscopic sensor 20 measures the Z-axis vibratory rate,
30 i.e., the rotation of the substrate about the axis normal to the micromachined surface 26 of substrate 24. The micromachined gyroscopic sensor 20 includes three major

elements: a suspension system 30, a drive system 32 used to sustain oscillation of proof mass 22 along the X-axis, and a sensing system 34 used both to detect deflections of proof mass 22 along the Y-axis and to apply
5 electrostatic forces to cancel any quadrature error, as will be described in detail below.

Referring to FIG. 3, suspension system 30 may be formed integrally with proof mass 22. Suspension system 30 supports the proof mass so that it may vibrate in a
10 plane parallel to surface 26. Suspension system 30 holds proof mass 22, for example, about two microns above the surface of the substrate. The total mass of proof mass 22 may be about 0.1 to 0.3 micrograms. Suspension system 30 is generally H-shaped, with two parallel beams 40 and
15 42 positioned generally along the X-axis. Each beam may be about 500 to 1000 microns in length, specifically about 800 microns in length. The end of each beam is connected to an anchor 44 which connects the suspension system to the substrate (see FIG. 2). The end of each
20 beam 40, as shown in FIG. 2, may include a folded or J-shaped flexure 45 (see FIG. 3). Alternately, beams 40 and 42 may be linear.

Two beams or crossbars 46 and 48 connect beam 40 to beam 42. Crossbars 46 and 48 may be about eight-
25 hundred microns long, and are positioned to trisect beams 40 and 42. Two cross-beams 50 and 52 connect crossbars 46 and 48. A third beam or crossbar 54 may connect the center of cross-beam 50 to the center of cross-beam 52. The flexible elements of suspension system 30 are
30 constructed of polysilicon and, for example, have a width and a thickness on the order of two microns. The anchors may be about eight microns square.

- 16 -

The suspension system 30 is designed to be flexible along the X-axis and Y-axis, and as rigid as possible to other modes of vibration. In particular, the suspension system must be substantially rigid to rotation

5 about the Z-axis, as small rotations may degrade the performance of the gyroscopic sensor. Large deflections may also result in the movable electrode fingers crashing into the stationary electrode fingers. The suspension system provides the necessary translational compliance

10 while maintaining rotational rigidity by thickening the portions of beams 40 and 42 located between crossbars 46 and 48 to form trusses 41 and 43. Trusses 41 and 43 may have a width three to four times the width of the remainder of the beams, i.e., about six to eight microns.

15 The portions of crossbars 46, 48 and 54 from which fingers project may have a width of approximately four microns.

The proof mass 22 also includes a plurality of finger electrodes (or simply fingers) which are used to

20 drive and sense oscillations of proof mass along the X-axis and Y axis. A plurality of long fingers 38 project outwardly along the X-axis from crossbars 46 and 48, and a plurality of short fingers or stubs 39 project inwardly along the X-axis from crossbars 46, 48 and 54. The

25 crossbars 46 and 48 form the spines, and long fingers 38 form the prongs of two movable sensing electrodes 56. Similarly, crossbars 46, 48 and 54 form the spines, and short fingers 39 form the prongs of two movable driving electrodes 58 and two movable feedback electrodes 59.

30 The short fingers 39 may be about ten to twenty-five microns in length, specifically fifteen microns in length, whereas the long fingers 38 may be about one-

- 17 -

hundred to two-hundred microns in length, specifically one-hundred and fifty microns in length.

Referring to FIG. 4, one or more stationary driving electrodes, one or more stationary feedback

5 electrodes, and one or more stationary sensing electrodes may be rigidly connected to substrate 24. For example, two stationary driving electrodes 60a, 60b may be arranged relative to each other in an opposing configuration. Similarly, two stationary feedback

10 electrodes 61a, 61b may face each other in an opposing configuration. Each stationary driving electrode 60a, 60b and each stationary feedback electrode 61a, 61b includes a plurality of short fingers 66. Stationary driving and feedback electrodes 60a, 60b and 61a, 61b may

15 have a few to dozens of fingers. Short fingers 66 may have a length of approximately 15 microns and a width of approximately three to six microns. The width, for example, may be four microns.

Two stationary sensing electrodes 62a, 62b may

20 face each other in an opposing configuration. Stationary sensing electrodes 62a, 62b include a plurality of long fingers 70. Each long finger 70 protrudes from a base 72. The fingers of stationary sensing electrode 62a are arranged in pairs, each pair including a right finger 74a

25 and a left finger 76a. Similarly, the fingers of stationary electrode 62b are arranged in pairs, each pair including a right finger 74b and a left finger 76b. Each long finger 70 may be approximately one hundred and fifty microns in length, and have a width of approximately four

30 microns.

Referring to FIG. 5, drive system 32 includes movable and stationary driving electrodes 58 and 60a, 60b, and movable and stationary feedback electrodes 59

- 18 -

and 61a, 61b. One set of short fingers 39 is
interdigitated with short fingers 66 of stationary
driving electrodes 60a, 60b. Another set of short
fingers 39 is interdigitated with short fingers 66 of
5 stationary feedback electrodes 61a, 61b. Short fingers
39 of movable electrodes 58 and 59, and short fingers 66
of stationary electrodes 60a, 60b and 61a, 61b may be
formed from the same layer of polysilicon prior to the
removal of the sacrificial layer so that the fingers may
10 be co-planar.

        The driving electrodes of drive system 32 act as
electrical-mechanical transducers. By the application of
an alternating voltage between stationary driving
electrodes 60a, 60b and movable driving electrodes 58,
15 proof mass 22 may be forced to oscillate or reciprocate
along the X-axis. The motion along the X-axis induces
bending in crossbars 46 and 48 so that proof mass 22 may
move toward and away from stationary driving electrodes
60a, 60b. A more detailed explanation of the manner of
20 operating drive system 32 in order to sustain
oscillations in proof mass 22 may be found in U.S. Pat.
No. 5,025,346, issued June 18, 1991 to Tang et al.,
entitled Laterally Driven Resonant Microstructures, and
assigned to the assignee of the present invention, the
25 entire disclosure of which is incorporated herein by
reference; and in U.S. Pat. No. 5,491,608, issued
February 13, 1996 to Nguyen, entitled Q-Controlled
Microresonators and Tunable Electronic Filters Using Such
Resonators, and assigned to the assignee of the present
30 invention, the entire disclosure of which is incorporated
herein by reference.

        Referring to FIG. 6, sensing system 34 includes
stationary sensing electrodes 62a, 62b and movable

- 19 -

sensing electrodes 56. The long fingers 38 of movable
sensing electrodes 56 and long fingers 70 of stationary
sensing electrodes 62a, 62b are interdigitated, with each
long finger 38 disposed between a right finger 74a, 74b
5 and a left finger 76a, 76b of sensing electrodes 62a,
62b. The spacing, Y_o, between fingers 70 and fingers 38
may be approximately one micron. Fingers 38 and 70 may
be formed from the same layer of polysilicon so that the
fingers are co-planar. Thus all of the driving and
10 sensing elements may be formed in the same fabrication
step. In addition, the driving mode and the sensing mode
operate in the X-Y plane parallel to the surface of
substrate 24. As will be described in more detail below,
sensing system 34 is used to sense the deflection of
15 proof mass 22 along the Y-axis, to apply electrostatic
forces to balance and eliminate the effect of quadrature
error, and to tune the resonant frequency of Y-axis
vibrations of the proof mass.

As discussed above, drive system 32 causes proof
20 mass 22 to oscillate along the X-axis. The position of
the proof mass along the X-axis, x(t), is given by the
following equation:

$$x(t) = X_0 \sin \omega_x t \tag{1}$$

where X_o is the amplitude of the oscillation and ω_x is the
frequency of the driving voltage (and thus the
25 oscillation frequency). The frequency of the driving
voltage, ω_x, may be between 7 kHz and 100 kHz, and the
driving voltage may be sufficient to cause the proof mass
to undergo a maximum deflection, X_o, of about one micron.
The magnitude of the Coriolis acceleration, $\ddot{y}_{Coriolis}$, is
30 given by the following equation:

- 20 -

$$\ddot{y}_{Coriolis} = 2 \cdot \Omega_z(t) \times \dot{x}(t) \qquad\qquad (2)$$

where $\Omega_z(t)$ is the rate of rotation of the proof mass
about the Z-axis and $\dot{x}$ is the velocity of the proof mass
along the X-axis. Equations 1 and 2 may be combined as
follows:

$$\ddot{y}_{Coriolis} = 2 \cdot \Omega_z(t) \cdot X_0 \cdot \omega_x \cdot \cos\omega_x t \qquad\qquad (3)$$

5   For a gyroscopic sensor with an oscillation amplitude $X_0=1$
μm, on oscillation frequency $\omega_x=20$ kHz, and an input
rotation rate $\Omega_z=1$ deg/sec, the Coriolis acceleration has
a magnitude of 0.45 milliG's.
        The Coriolis acceleration is an amplitude-
10 modulated signal in which the carrier frequency is the
oscillation frequency and the rotation rate modulates the
amplitude. The resulting Coriolis acceleration is a dual
sideband signal centered on the oscillation frequency.
Referring to FIG. 7A, since the Y-axis accelerations are
15 proportional to velocity, the motion of proof mass 22 is
elliptical. The maximum deflection of proof mass 22
along the Y-axis will be a few nanometers. The
deflection detectable by gyroscopic sensor 20 may be on
the order of a picometer.
20   In an ideal device, the moving electrodes are
perfectly aligned with the stationary electrodes so that
the only motion caused by drive system 32 is along the X-
axis. However, one effect of manufacturing flaws is
quadrature error. Referring to FIG. 7B, quadrature error
25 occurs if proof mass 22 oscillates along an axis that is
not exactly parallel to the X-axis. If this is the case,
then there is some small fraction, ε, of the drive
oscillation, X(t), which lies along the Y-axis. This

- 21 -

quadrature displacement along the Y-axis is given by the following equation:

$$Y_{Quadrature} = -\varepsilon \cdot x(t) \tag{4}$$

If this displacement is differentiated twice, the acceleration, $\ddot{y}_{quadrature}$, due to off-axis oscillation can be
5 determined. This acceleration, given in Equation 5 below, is referred to as quadrature error.

$$\ddot{Y}_{Quadrature} = \varepsilon \cdot X_0 \cdot \omega_x^2 \cdot \sin\omega_x t \tag{5}$$

Note the similarity between the quadrature error and the Coriolis acceleration: both are sinusoidal signals centered at the frequency of oscillation.
10 However, the signals can be distinguished by their phase relative to the driven oscillation. Specifically, the Coriolis acceleration is ninety degrees out of phase relative to the drive oscillation, ω_x, whereas the quadrature error is in phase with the driven oscillation.
15 The quadrature error can be quite large. In fact, the quadrature error may easily exceed the Coriolis acceleration. The ratio of quadrature error and Coriolis acceleration is given by Equation 6:

$$\frac{\ddot{y}_{Coriolis}}{\ddot{y}_{Quadrature}} = \frac{2\Omega_z(t) \cdot X_0 \cdot \omega_x}{\varepsilon \cdot X_0 \cdot \omega_x^2} = \frac{2\Omega_z(t)}{\varepsilon \cdot \omega_x} \tag{6}$$

Using the previous example of an input rotation
20 rate, Ω_z, of 1 deg/sec and an oscillation frequency, ω_x, of 20 kHz, for the quadrature error to be as small as the Coriolis acceleration, the oscillation direction must be accurate to a factor of 1 part in 3.6 million. Due to manufacturing flaws and other imbalances, the quadrature
25 error may be considerably larger than this. Accordingly,

- 22 -

gyroscopic sensor 20 has a mechanism to reduce, or
nullify the quadrature error.

Microfabricated gyroscopic sensor 20 may apply
electrostatic forces to proof mass 22 through sensing
5 system 34. By selection of the proper electrostatic
force, the quadrature error may be nullified. As shown
by Equation 5, the quadrature error is directly
proportional to position of the proof mass along the X-
axis. To cancel this error signal without effecting the
10 Coriolis signal, a balancing force must be applied that
is also directly proportional to the position of the
proof mass along the X-axis. Gyroscopic sensor 20
applies such a balancing force, using the interdigitated
Y-axis position sense fingers.
15   Referring to FIG. 7C, proof mass 22 is shown with
two fingers 38a and 38b projecting from opposite sides of
the proof mass. Finger 38a is surrounded by right and
left fingers 74a and 76a, whereas finger 38b is
surrounded by right and left fingers 74b and 76b. A
20 small voltage differential, $2\Delta V$, is applied between the
right finger 74a and left finger 76a. The opposite
voltage potential $-2\Delta V$, may be applied between right
finger 74b and left finger 76b. This voltage difference
creates a balancing force, F_y, which counteracts the
25 quadrature error. The balancing force acts on proof mass
22 so that, absent the Coriolis force, fingers 39 vibrate
solely along the X-axis. As mentioned above, the
balancing force needs to be exactly proportional to the
position of the proof mass along the X-axis. An
30 electrostatic force between two charged surfaces is
proportional to the overlapping area of the surfaces.
Because the overlapping area between fingers 38 and
fingers 70 is directly proportional to the position of

- 23 -

proof mass 22 along the X-axis, as proof mass oscillates,
the position sense capacitors change proportionately.
Therefore, the electrostatic balancing force F_y will also
be proportional to the position of proof mass 22.

5   Sensing system 34 applies a DC bias voltage V_{DC} to fingers
74a, 74b, 76a and 76b and a voltage differential $2\Delta V$
between fingers 74a, 74b and 76a, 76b given by Equation 7
below:

$$F_y = \frac{C_{overlap}}{y_0} x(t) \cdot ((V_{DC}+\Delta V)^2 - (V_{DC}-\Delta V)^2) = 2\frac{C_{overlap}}{y_0} V_{DC}\Delta V \cdot x \qquad (7)$$

where $C_{overlap}$ is the maximum change in capacitance between
10 fingers 70 and fingers 38 as the structure oscillates and
y_0 is the equilibrium distance between fingers 70 and
fingers 38.

By properly selecting the voltage differential ΔV,
the quadrature error may be significantly reduced, e.g.,
15 by a factor ten to one-hundred. The proper voltage
difference may be calculated from Equations (7) and (5)
and Newton's law   F = ma, as follows:

$$\Delta V = M\frac{\varepsilon y_0 \omega_x^2}{V_{DC}C_{overlap}} \qquad (8)$$

where M is the mass of proof mass 22. Because the
quadrature error is a result of manufacturing defects,
20 the proper voltage differential depends upon the specific
structure and may vary from device to device. A voltage
differential in the range of 1 mV to 100 mV should be
appropriate. The optimum voltage differential to cancel
the quadrature error may be determined experimentally
25 (see FIG. 13 which is discussed below).

- 24 -

In addition to canceling the quadrature error,
sensing system 34 of gyroscopic sensor 20 may be used to
match the Y-axis resonant frequency ω_y of proof mass 22 to
the driving oscillating frequency ω_y. Because gyroscopic
5   sensor 20 is a high Q second order system, the response
of proof mass 22 to Coriolis acceleration can be
enhanced. As shown by Equation 3, the Coriolis
acceleration is a signal centered around the oscillation
frequency ω_x. Therefore the relative values of the
10 oscillation frequency ω_x and the Y-axis resonant frequency
ω_y have a dramatic effect on the response of the sense
mode and hence the sensor sensitivity. If the Y-axis
resonant frequency is matched to the oscillation
frequency, the device may experience a gain of Q in the
15 system response. However, the bandwidth of the sensor is
then limited to ω_y/Q. Given that system is run in a
vacuum and Q is typically greater than 10,000, the system
bandwidth for $\omega_x=\omega_y$ will be only a few Hertz.

For larger bandwidth and increased sensitivity,
20 gyroscopic sensor 20 is operated with a slight mismatch
between resonant frequency ω_y and oscillation frequency
ω_x. The system response of Y-axis displacement due to
Coriolis acceleration is given by:

$$\frac{y}{\Omega_z} = \frac{2X_0\omega_x\sin\omega_x t}{\omega_y^2 + \dfrac{j\omega_x\omega_y}{Q} - \omega_x^2} = \frac{X_0\omega_x}{\omega_x\Delta\omega}\sin\omega_x t \qquad (9)$$

Provided that there is a means to tune the Y-axis
25 resonant frequency, it is desirable to operate the
gyroscopic sensor with a 5-10% frequency mismatch, $\Delta\omega/\omega_x$,
yielding a gain of 5-10 in sensitivity. For example, if
ω_x is about 12 kHz, then ω_y may be set to about 12.5 kHz.
Alternately, the frequency mismatch may be reduced to

- 25 -

about 1-2%. Reducing the mismatch further might increase
the sensitivity but may be difficult to maintain for any
length of time because the resonant frequency changes as
the temperature of the gyroscopic sensor changes.

5   Tuning of the Y-axis resonant to improve
sensitivity is accomplished using electrostatic
"negative" springs, i.e., by applying a DC bias voltage,
V_{DC}, between proof mass 22 and stationary sensing
electrodes 62. When the DC voltage is established
10 between the moving proof mass and the stationary sensing
electrode, the resulting attractive force reduces the
total spring constant and thus adjusts the resonant
frequency.

          Using a first-order model for the parallel-plate
15 capacitors, the linearized spring force due to
electrostatic forces is given by:

$$F_y = [\frac{1}{(y_0-y)^2} - \frac{1}{(y_0+y)^2}] \frac{y_0 C_s V_{DC}^2}{2} \qquad (10)$$

where y is the deflection of the proof mass along the Y-
axis away from its equilibrium position.

          The Y-axis resonant frequency, ω_y, is given by the
20 following equation:

$$\omega_y = \sqrt{\frac{k_y + k_e}{M}} \qquad (11)$$

where k_y is the purely mechanical spring constant, k_e is
the electrostatic spring constant and M is the mass of
proof mass 22. The mechanical spring constant k_y is
primarily a function of the stiffness of suspension
25 system 30.

- 26 -

The electromagnetic spring constant, k_e, is given by the following equation:

$$k_e = -2\frac{C_s}{y_0^2}V_{DC}^2 \tag{12}$$

in which C_s is the sense capacitance of the gyroscopic sensor and y_0 is the distance between fingers 38 and 70
5   (see FIG. 7A). C_s depends upon the total number of fingers and the amount of overlapping area, and should be at least 30 femtoFarads (fF). By increasing the number of fingers, C_s may be increased to about one picoFarad (pF). As mentioned above, the spacing y_0 between fingers
10 is about one micron. It may be noted that k_e has a negative value, so that as V_{DC} is increased ω_y is decreased. The system starts with ω_y larger than ω_x, and the bias voltage V_{DC} is increased, thereby reducing ω_y, until the desired mismatch $\Delta\omega/\omega_y$ is achieved. The correct
15 valve for V_{DC} may be determined experimentally (see FIG. 12 which is discussed below), but should be in the range of one to ten volts.

In addition to canceling the quadrature error and adjusting the Y-axis resonant frequency, sensing system
20 34 may be used to negate the effects of centrifugal or centripetal force. As the gyroscope sensor rotates about the Z-axis, a centrifugal force will push the proof mass outwardly (assuming the axis of rotation does not pass exactly through the center of mass of the proof mass). A
25 voltage difference, V_c, may be applied between the opposing stationary sensing electrodes 62a and 62b. Because the centripetal force varies at a low frequency, compared to the frequencies of the Coriolis force, a high pass filter may be used to remove the effect of the
30 centripetal force from the output.

- 27 -

Gyroscopic sensor 20 measures the position of proof mass 22 along the Y-axis by capacitive deflection sensing. The interdigitated fingers of sensing system 34 (shown in FIG. 2) are used to sense deflection of the

5   proof mass along the Y-axis. The fingers are arranged in a capacitor bridge so that any deflection of the proof mass results in measurable changes in the relative size of the capacitors. In a first order model, the capacitance of a parallel-plate capacitor is inversely

10 proportional to the distance between the plates.

Referring to FIGS. 6 and 8A, the space between finger 38 of movable sensing electrode 56 and right fingers 74a, 74b of sensing electrodes 62a, 62b forms a first capacitor C_1, and the space between finger 38 and

15 left fingers 76a, 76b forms a second capacitor C_2. As movable sensing electrode 56 is deflected along the Y-axis, C_1 and C_2 change. For example, if sensing electrode 56 is deflected leftward, the distance between finger 38 and right fingers 74a, 74b increases, thereby decreasing

20 C_1, while the distance between finger 38 and left fingers 76a, 76b decreases, thereby increasing C_2. The change in capacitance is detected by a position sensor 80, such as an integrator or voltage buffer, which includes an amplifier 82. Finger 38 is connected to the negative

25 input of amplifier 82. The output of amplifier 82 is connected to the negative input of the amplifier via an integrating capacitor 84 to form an integrator. The negative input of amplifier 82 is connected to ground via a parasitic capacitor 83. The positive input of

30 amplifier 82 may be connected directly to ground.

Because capacitance cannot be measured with a DC voltage, a voltage source 90 applies an AC voltage V_s between fingers 74a, 74b and 76a, 76b. The voltage V_s is

- 28 -

about 0.1 to 5.0 volts, preferably about one volt, and
has a frequency much higher than the driving frequency ω_x.
For example, the frequency of voltage source 90 may be
about one megahertz.

5   The integrator shown in FIG. 8A offers the
flexibility of trading bandwidth for sensitivity by
varying the integrating capacitor size. The integrator
also provides lower distortion. Some of the parasitic
capacitors involved in microelectromechanical systems are
10 nonlinear which will vary the gain of a buffer and
thereby result in distortion, and the practice of
bootstrapping parasitic capacitance is a form of positive
feedback which exacerbates amplifier distortion.
However, because the integrator uses a fixed, linear
15 capacitor, distortion is kept to a minimum.

        Another common amplifier configurations used for
capacitive position sensing is shown in FIG. 8B, in which
the output of amplifier 82 is connected to its negative
input and sensing electrodes 56 are connected to the
20 positive input of the amplifier to form a voltage buffer.

        Unfortunately, the integrator presents a difficult
biasing problem. Ideally, biasing can be performed by
placing a very large resistor in parallel with the
integrating capacitor. However, any practical
25 implementation of a large resistor results in a
considerable parasitic capacitance. A diode can also be
used in parallel with the integrating capacitance;
however, that adds a nonlinear capacitance to the
integrating capacitance resulting in distortion.
30 Referring to FIG. 8C, this biasing problem has been
solved by using a subthreshold metal oxide semiconductor
field effect transistor (MOSFET) 88. The MOSFET device
is connected in parallel with integrating capacitor 84 so

- 29 -

that the source of MOSFET 88 is connected to the output
of amplifier 82, the drain is connected to the negative
input of amplifier 82, and the gate is connected to
ground. The negative input of amplifier 82 may be
5 connected to ground by a diode 86, and the positive input
of amplifier 82 may be connected directly to ground. In
the subthreshold regime, the MOSFET device exhibits
extremely low transconductance and no source-to-drain
capacitance. The use of subthreshold MOSFET device has
10 resulted in a well behaved integrator operable down to 1
kHz with a 50 F integrating capacitor without additional
noise or distortion attributable to the bias circuitry.

Referring to FIG. 9, gyroscopic sensor 20 includes
a phase-locked loop (PLL) 100 and several synchronous
15 demodulators or mixers to perform signal processing.
Phase-locked loop 100 produces extremely accurate digital
signals having a driving frequency ω_x between about 7 kHz
and 100 kHz. The drive frequency, ω_x, may be generated by
dividing down the signal from voltage source 90. The
20 phase-locked loop ensures that the position signals are
exactly in phase with the position of proof mass 22.
Phase-locked loop 100 may also generate a velocity signal
on line 108 which is exactly ninety degrees out of phase
with a position signal on line 110. Position signals on
25 lines 102 and 104, having opposite amplitudes, are
supplied by phase-locked loop 100 to the positive and
negative outputs, respectively, of a transresistance
amplifier 106. Opposing stationary drive electrodes 60a
and 60b are also connected to the positive and negative
30 outputs of transresistance amplifier 106. Opposing
feedback electrodes 61a and 61b are connected to the
positive and negative inputs of transresistance amplifier
106. One of the outputs of transresistance amplifier 106

- 30 -

is mixed with the velocity signal by a mixer 112. The
combined output of mixer 112 is applied to trans-
resistance amplifier 106 to provide an automatic gain
control (AGC) circuit to control the amplitude of the
5 oscillations of proof mass 22 along the X-axis. The
phase accuracy of the phase-locked loop is critical to
the operation of gyroscopic sensor 20 because any phase
error will result in cross-talk between the Coriolis and
quadrature signals. Assuming that a phase error $\theta_n(t)$ is
10 generated by phase noise in the phase-locked loop, the
error in the rotation rate Ω may be derived as shown in
Equations 13-15 below:

$$y(t) = [\frac{X_0\omega_x}{\omega_x\Delta\omega}\Omega\cos\omega t + Y_{Quadrature}\sin\omega t] \tag{13}$$

$$\Omega_{est} = \frac{\omega_x\Delta\omega}{X_0\omega_x}y(t)\cos(\omega_x t+\theta_n(t)) \tag{14}$$

$$\Omega_{est} = \Omega + \frac{\omega_x\Delta\omega}{X_0\omega_x}Y_{Qadrature}\theta_n(t) + \textit{Higher terms} \tag{15}$$

Because phase-locked loop 100 is extremely accurate,
phase noise is minimized and variable cross-talk is
15 extremely small. In addition, quadrature error
correction reduces cross talk and phase noise.
        The nulling of the quadrature error, the tuning of
the Y-axis resonant frequency, and the balancing of the
centrifugal forces is accomplished by the application of
20 the proper voltages to fingers 70 of opposing stationary
sensing electrodes 62a and 62b. Specifically, gyroscopic
sensor 20 includes four DC bias voltage sources 120, 122,

- 31 -

124 and 126. Voltage source 120 applies a total voltage $V_t=V_{DC}+\Delta V+V_c$ to right fingers 74a of sensing electrode 62a. Voltage source 122 applies a total voltage of $V_{DC}-\Delta V-V_c$ to left fingers 76a. Voltage source 124 applies a total

5   voltage of $V_{DC}-\Delta V+V_c$ to right electrode fingers 74b of sensing electrode 62b. Voltage source 126 applies a total voltage of $V_{DC}+\Delta V-V_c$ to left fingers 76b. Thus, voltage sources 120, 122, 124 and 126 provide all of the necessary bias voltages in order to nullify the

10 quadrature error, select the desired Y-axis resonant frequency, and cancel any centrifugal or other low-frequency forces. Of course, any other combination of voltage sources providing the same effective total voltage to the fingers of the sensing electrodes could be

15 used. Also, the voltages could be applied by different sets of fingers of the stationary sensing electrode, for example, V_{DC} could be applied by one set of fingers and ΔV could be applied by another set of fingers.

In order to extract the position, Coriolis effect,

20 and quadrature signals from capacitive position sensor 80, the signal from amplifier 82 is boosted by an oscillation amplifier 130 to produce an output signal on line 132. This output signal may be mixed with signals from a modulator or clock and the position and velocity

25 signals from phase locked loop 100. Voltage source 90 may produce a high frequency, e.g., one megahertz clock signal on line 134. To generate the position signal, this clock signal is mixed with the output signal on line 132 by a mixer 136. In order to produce the Coriolis

30 signal, the clock signal on line 134 is mixed with the velocity signal on line 108 by a mixer 140 to produce a combined signal on line 142. The combined signal on line 142 is then mixed with output signal on line 132 by a

- 32 -

mixer 144 to produce the Coriolis signal. Finally, to
produce the quadrature signal, the clock signal on line
134 is mixed with the position signal on line 110 by a
mixer 150 to produce a combined signal on line 152. The
5 combined signal on line 152 is then mixed with output
signal on line 132 by a mixer 154 to produce the
quadrature signal. The position, Coriolis and quadrature
signals may be passed through low pass filters to filter
out high frequency components.

10   Referring to FIG. 10, a gyroscopic sensor 20 was
fabricated on a silicon substrate 24 using a combination
of metal oxide semiconductor and microelectromechanical
fabrication techniques. The transresistance amplifier
and integrator were fabricated on the same die, and the
15 remaining electronics was implemented off of the chip.
The mechanical sensing element is about one millimeter
across.

          There are a number of possible noise sources in
gyroscopic sensor 20. Principal among these are:
20 Brownian noise, op-amp noise in the integrator, and phase
locked loop phase noise. The Brownian noise, $\Omega_n B$,
represents the fundamental limit on angular rate
resolution and is given by:

$$\Omega_{nB} = \sqrt{\frac{kT\omega_y BW}{MQ\omega_x^2 X_0^2}} \qquad (16)$$

where k is Boltzman's constant, T is the temperature, M
25 is the mass of the proof mass, BW is the bandwidth of the
gyroscopic sensor, and Q is the quality factor. As an
example, consider a gyroscopic sensor with mass, M=0.2µg,
an oscillation amplitude X_0=1 µm, a quality factor, Q=
10,000, a bandwidth BW = 100 Hz, a drive frequency ω_x= 20

- 33 -

kHz and a resonant frequency ω_y= 20 kHz. For this
example, we find a Brownian noise floor Ω_{nB}=0.06 deg/sec.
Because the gyroscopic sensor is run in vacuum and has a
high Q, Brownian noise is not the dominant noise source.

5   As shown by Equation 15, phase noise in the phase
locked loop, represented by $\theta_n(t)$, can cause variable
cross talk between quadrature and Coriolis signals. In
gyroscopic sensor 20, this effect is kept to a minimum
due to the low phase noise in the phase locked loop and
10 nulled quadrature error.

           The integrator op-amp noise is the dominant noise
source in gyroscopic sensor 20. The input-referred
noise, Ω_E, of the op-amp noise is a function of the total
capacitance, C_T, attached to the summing node of the
15 integrator, and is given by:

$$\Omega_{nE} = \frac{C_T y_0 \nu_n}{C_s X_0 V_s} \Delta\omega\sqrt{2BW} = \frac{y_0 \Delta\omega}{X_0 V_s}\sqrt{\frac{32kTBW}{3\pi C_s f_T}} \tag{17}$$

where f_T is the maximum operable frequency of the
transistors in gyroscopic sensor 20. The electronic
noise is at best Ω_{nE}=0.08 deg/sec for a modest CMOS
process with f_T=250 MHZ, a frequency mismatch $\Delta\omega$=1 kHz, a
20 sense voltage V_s=1 volt, a sense capacitance C_s=100fF, and
the oscillation amplitude and finger spacing $X_0=y_0$=1 µm.

           An initial characterization of the gyroscopic
sensor response is shown in FIG. 11. FIG. 11 is a graph
of the logarithm of the output voltage of the Coriolis
25 signal, on the Y-axis, as a function of frequency, on the
X-axis. The graph was produced by measuring the output
Coriolis signal in response to a 1Hz, 5 deg/sec sine wave
rotation. The gyroscopic sensor was operated with an
oscillation frequency, ω_x, of 12 kHz and a Y-axis resonant
30 frequency, ω_y, of about 12.5 kHz. The noise floor for

- 34 -

this version of Z-axis vibratory rate gyroscopic sensor
is 1 deg/sec/Hz$^{\text{½}}$.

Referring to FIG. 12, there is a measured
mechanical resonant frequencies of proof mass 22 as a
5 function of the DC bias voltage applied to the position
sense fingers. FIG. 12 shows a graph of the resonant
frequencies of proof mass 22 (on the Y-axis of the graph)
as a function of the RMS voltage (on the X-axis of the
graph) applied between fingers 38 and fingers 70. The
10 RMS voltage is a combination of the DC bias voltage and
the AC voltage generated by voltage source 90. The
resulting electrostatic springs reduce the resonant
frequency of the sense mode (ω_y), raise the resonant
frequencies of the out-of-plane modes, and leaves the
15 driven mode (ω_x) unaffected. As expected, the Y-axis
resonant frequency drops as the bias voltage is increased
and the oscillation frequency of proof mass 22 remains
constant at 12kHz. The resonant frequencies of the
vertical and tipping modes increase with DC bias due to
20 electrostatic levitation effects.

As discussed above, gyroscopic sensor 20 includes
a means to null quadrature error. FIG. 13 shows a graph
of the measured voltage, V_{out} on the Y-axis, as a function
of the voltage differential, ΔV, on the X-axis, which is
25 applied between right fingers 74a, 74b and left fingers
76a, 76b. Both the quadrature and rotation rate signals
were plotted for a zero rotation rate as ΔV was adjusted.
Measurements of the quadrature error and rotation rate
signals demonstrate that the quadrature error signal can
30 be controlled independently of the Coriolis signal.

Another embodiment of the gyroscopic sensor, in
which the sensing and quadrature correction voltages are
applied by different electrode fingers, is shown by FIG.

- 35 -

14.   Referring to FIG. 14, a micromachined gyroscopic
sensor 200 includes a proof mass 202 connected to a
substrate 204 by a suspension system 206. The gyroscopic
sensor 200 includes three major electronic elements: a
5 drive system 210 used to sustain oscillation of proof
mass 202 along the X-axis, a sensing systems 212 used to
detect deflections of proof mass 202 along the Y-axis,
and a quadrature correction system 214 used to cancel any
quadrature error.

10   The proof mass 202 includes a rectangular outer
stage 220 and a rectangular inner stage 222. Each corner
of outer stage 220 is connected by a folded or J-shaped
first flexure 224 to an anchor 226 which secures proof
mass 202 and suspension system 206 to substrate 204.
15 Similarly, each corner of inner stage 222 is connected to
outer stage 220 by a second flexure 228. The first
flexure 224 is designed to permit outer stage 220 to
vibrate primarily along a Y-axis with respect to
substrate 204, whereas second flexure 228 is designed to
20 permit inner stage 222 to vibrate substantially along the
X-axis with respect to outer stage 220. Several beams or
crossbars 230 may connect opposing sides of inner stage
222.

          The physical characteristics of gyroscopic sensor
25 200 are similar to those of gyroscopic sensor 20. The
sensor may be about 0.5 to 2.0 millimeters on a side; the
proof mass may have a total mass of about 0.1 to 0.5
micrograms; the flexible elements of the suspension
system may be constructed of polysilicon and may have a
30 width and a thickness on the order of two microns. The
entire assembly may be fabricated using traditional
integrated circuit fabrication techniques.

- 36 -

Referring to FIG. 14, the drive system 210 includes two driving electrodes 232a and 232b, and two feedback electrodes 234a and 234b, all connected to substrate 204. A plurality of electrode fingers 236

5 project along the X-axis from each feedback electrode and each drive electrode. A plurality of electrode fingers 238 project from inner stage 222 of proof mass 202 along the X-axis, and are interdigitated with electrode fingers 236 of the sense and drive electrodes.

10 As shown in FIG. 15, feedback electrodes 234a and 234b are connected to the positive and negative inputs, respectively, of a transresistance amplifier 240. The driving electrodes 232a and 232b are connected to the positive and negative outputs of transresistance

15 amplifier 240, respectively, and to a phase-locked loop 242, as previously described with respect to FIG. 9.

The sensing system 212 includes a plurality of pairs of sense electrodes fingers aligned with the X-axis. Each pair of sense electrode fingers includes a

20 right finger 244 and a left finger 246. A plurality of electrode fingers 248 are connected to outer stage 220 and are interdigited so that each electrode finger 248 is disposed between one right finger 244 and one left finger 246. A sense voltage source 250 (see FIG. 15) applies an

25 AC voltage between the right fingers 244 and the left fingers 246.

Quadrature correction system 214 includes several sets of correction electrodes positioned near the center-line of the sensor and connected to the substrate. Each

30 set of correction electrodes includes an upper left electrode 260, an upper right electrode 262, a lower left electrode 264, and a lower right electrode 266. Upper right electrode 262 and lower left electrode 264 may be a

- 37 -

single electrode, as shown, or may be separate
electrodes. A plurality of electrode fingers 268 extend
from crossbars 230 and are interdigited with the
connection electrodes. Specifically, each electrode
5 finger 268 extends along the X-axis from crossbar 230 and
is disposed between upper left electrode 260 and upper
right electrode 262. Similarly, each electrode finger
268 extends along the X-axis from crossbar 230 and is
disposed between lower left electrode 264 and lower right
10 electrode 266. Upper left electrode 260 is electrically
connected to lower right electrodes 266, and upper right
electrode 262 is electrically connected to lower left
electrode 264.

       A voltage source 270 (FIG. 15) applies a DC bias
15 voltage between the correction electrodes 260, 266 and
262, 264. The voltage differential between the left and
right electrodes creates a balancing force to counteract
the quadrature error as discussed with respect to FIG.
7C. The remainder of the circuitry, including an
20 integrator 280 and mixers 282-286 may be assembled and
function in a manner similar to the circuitry discussed
above with reference to FIG. 9.

       Referring to FIG. 16, quadrature correction may be
used to compensate for manufacturing flaws that occur in
25 the fabrication of other sorts of gyroscopic sensors,
such as X-axis and Y-axis gyroscopic sensors. A dual-
axis vibratory gyroscope functions by generating and
sensing Coriolis accelerations. The functional operation
of the dual-axis vibratory gyroscope is illustrated by an
30 equivalent spring-mass system. In a dual-axis gyroscopic
sensor 290, a proof mass 292 is supported by a flexible
suspension 294 from a frame 296. The proof mass is
generally disc-shaped, and lies in a plane generally

- 38 -

parallel to the surface of the substrate. The proof mass
is oscillated about the Z-axis (the axis perpendicular to
the surface of the substrate) by a drive torque F_d with a
frequency ω_z. If the frame rotates about a first axis
5 parallel to the surface of the substrate, e.g., the Y-
axis, at a rotation rate Ω_Y, then the combination of this
rotation and oscillation generates an oscillating
Coriolis torque F_c about a second axis parallel to the
surface of the substrate and perpendicular to the first
10 axis, i.e., the X-axis. This Coriolis force torque will
tend to oscillate the proof mass about the X-axis at a
frequency ω_x. Thus, rotation of the proof mass about the
Y-axis causes the proof mass to undergo a "see-saw"
motion about the X-axis. Similarly, a rotation about the
15 X-axis will induce a Coriolis oscillation about the Y-
axis.

The Coriolis acceleration about the X-axis
generated by rotation of the proof mass about the Y-axis
is given by the following equation:

$$I_{xx}\ddot{\theta}_x + C_x\dot{\theta}_x + K_x\theta_x = -I_{zz}\Omega_y \times \theta_{z0}\omega_z \cos(\omega_z t) \qquad (18)$$

20 where θ_x is the sense-axis tilt angle, I_{xx} is the X-axis
moment of inertia, C_x is the damping co-efficient, K_x is
the spring constant, ω_z is the frequency of oscillation
about the Z-axis, I_{zz} is the Z-axis movement of inertia,
and Ω_y is the rotation rate of the proof mass about the Y-
25 axis. The angular oscillation of the rotor caused by the
Coriolis acceleration can be thought of as an amplitude
modulated signal with a carrier frequency ω_z. The
amplitude of the modulated signal is directly
proportional to the Y-axis rotation rate Ω_y. The equation
30 for Coriolis acceleration about the Y-axis is essentially

- 39 -

identical except that the x and y subscripts are reversed
and the right-hand side of the equation is positive.

Referring to FIG. 17A, a dual-axis gyroscopic
sensor 300 includes a generally ring-shaped proof mass
5   302 connected to a rigid frame or substrate 304 by a
suspension system 306. Dual-axis gyroscopic sensor 300
measures the X-axis and Y-axis rotation rate; i.e., the
rotation of the substrate about the axes parallel to the
surface of substrate 304. Dual-axis gyroscopic sensor
10 300 includes three major electronic elements: a drive
system 310 used to sustain oscillation of proof mass 302
about the Z-axis, a sensing system 312 used to detect
deflections of proof mass 302 about the X-axis and Y-
axis, and a quadrature correction system 314 used to
15 cancel any quadrature error. The dual-axis gyroscopic
sensor 300 may be fabricated using standard integrated
circuit techniques.

The proof mass 302 includes a generally ring-
shaped rotor 316. Rotor 316 may be a two micron thick
20 polysilicon ring with an outer radius of about 250
microns and an inner radius of about 200 microns. The
proof mass 302 is substantially symmetric about the X-
and Y-axis.

The suspension system 306 may include four beams
25 320 which connect an inner edge 322 of the proof mass to
an anchor 324 which secures rotor 316 to substrate 304.
The beams 320 may also be constructed of polysilicon and
may have a width and thickness on the order of two
microns.

30   Alternately, the suspension system may include a
serpentine suspension with folded beams. In yet another
version, the proof mass may be suspended by four beams
connected to an outer edge of the rotor. A serpentine

- 40 -

suspension system provides a lower natural frequency and can accommodate warping of the rotor.

Suspension systems 306 is designed to provide a torsional suspension for rotor 316 to allow rotation
5 about the three perpendicular axes. However, suspension system 306 is designed to be rigid to translational accelerations along the X-axis and the Y-axis. Although rotor 316 may undergo translational acceleration along the Z-axis, the differential sensing scheme discussed
10 below substantially cancels sensitivity to such accelerations.

For maximum mechanical sensitivity, the suspension system is designed to match the frequencies of all three rotational modes sufficiently well that electrostatic
15 tuning may compensate for process variations during manufacture of the gyroscope sensor. In particular, the sense axis natural frequencies were designed to be about ten percent above the drive natural frequencies so that the sense frequencies may be down tuned to match the
20 drive frequency.

A plurality of inner combs 330a-330d project inwardly from inner edge 322 of rotor 316. Each inner comb includes a spine 332 and a plurality of teeth 334 which project from both sides of the spine. The number
25 and configuration of inner combs in FIG. 17A is merely illustrative. The dual axis gyroscope may include twelve inner combs, each having five teeth. Four outer combs 340a-340d project outwardly from an outer edge 326 of rotor 316. Each outer comb includes a spine 342 and a
30 plurality of teeth 344 projecting from both sides of the spine. Although teeth 334 and 344 in FIG. 17A are illustrated as linear, as shown in FIG. 17B it is

advantageous for the teeth to be constructed as portions
of arcs from concentric circles.

     As previously mentioned, drive system 310 induces
oscillations of proof mass 302 about the Z-axis. The
5 drive system 310 includes one or more drive electrodes
350a-350b and one or more feedback electrodes 352a-352b
connected to substrate 304. Preferably, the drive and
feedback electrodes are arranged in opposing pairs
located on either side of each inner comb 330a-330d.
10 Each feedback and drive electrode includes a plurality of
teeth 354 which are interdigited with teeth 334 of the
adjacent inner comb.   Teeth 354 may have an arc length
of approximately twenty microns and a width of
approximately two microns. The drive electrodes of drive
15 system 310 act as electrical, mechanical transducers. By
application of an alternating voltage between the drive
electrodes and the proof mass, the proof mass may be
forced to oscillate about the Z-axis. Specifically,
beams 320 may flex or bend so that rotor 316 may rotate.
20   Referring to FIG. 18, dual-axis gyroscopic sensor
300 includes a transresistance amplifier 366 which
produces drive signals 362 and 364 having a driving
frequency ω_z of about twenty to thirty kilohertz. Drive
signals 362 and 364 are equal in magnitude but opposite
25 in sign. phase-locked loop 360. A phase-locked loop
360 generates an extremely accurate digital output signal
on line 368 which is in phase with the rotational rate of
the proof mass. The opposing feedback electrodes 352a
and 352b are connected to the positive and negative
30 inputs of trans-resistance amplifier 366. The opposing
drive electrodes 350a and 350b are connected to the
positive and negative outputs 362 and 364 of trans-
resistance amplifier 366 and to phase-locked loop 360.

- 42 -

The positive and negative outputs of trans-resistance
amplifier 366 are also mixed with the digital output
signal on line 368 by a mixer 370. The output of mixer
370 is then used to modulate trans-resistance amplifier
5 366. This modulation provides an automatic gain control
circuit to control the amplitude of the oscillations of
proof mass 302. Thus, drive system 310 provides a phase-
locked oscillation of constant amplitude to the proof
mass and provides a clean signal for Coriolis
10 demodulation.

Returning to FIG. 17A, sensing system 312 includes
four sense electrodes 374a-374d (shown in phantom because
they are located beneath the rotor 316). Each sense
electrode is shaped as a quarter-pie section and may be
15 formed of an n+ diffused region in substrate 304. Sense
electrodes 374a and 374c are positioned along the X-axis
whereas the sense electrodes 374b and 374d are positioned
along the Y-axis. The Coriolis oscillation is measured
by sensing the change in capacitance between rotor 316
20 and sense electrodes 374a-374d. For example, if the
gyroscopic sensor rotates about the Y-axis, then the
Coriolis force may cause the right portion of rotor 316
to move closer to sense electrode 374b and the left
portion of rotor 316 to move farther away from sense
25 electrode 374d. Thus, the capacitance between sense
electrode 374b and rotor 316 increases whereas the
capacitance between sense electrode 374d and rotor 316
decreases. Because each pair of opposing sense
electrodes provides differential sensing, translation of
30 the rotor up or down along the Z-axis does not change in
sense output.

Referring to FIG. 18, a first sense voltage source
376 connects opposing sense electrodes 374a and 374c, and

- 43 -

a second sense voltage source 378 connects opposing sense
electrodes 374b and 374d. The sense voltage sources 376
and 378 generate AC voltages with different modulation
frequencies. For example, one voltage source may operate
5 at 200 kHz and the other voltage source may operate at
300 kHz. In order to extract the position signals
indicating the angular position of rotor 316 about the X-
axis and Y-axis, proof mass 302 is electrically connected
to an integrator 380. The integrator 380 may include a
10 capacitor 381 having a capacitance of about 50
femtoFarrads. A benefit of integrator 380 is that it
improves linearity.

The output of integrator 380 is demodulated with
the signal from sense voltage source 376 by a mixer 382.
15 The output from integrator 380 is also demodulated with
the signal from sense voltage source 378 by a mixer 384.
The outputs of mixers 382 and 384 are then demodulated by
mixers 386 and 388 with the digital output signal on line
368 from phase-locked loop 360. The output of mixer 386
20 provides the angular rotation rate of the gyroscopic
sensor about the X-axis, and the output of mixer 388
provides the rotation rate of the gyroscopic sensor about
the Y-axis.

The combined mechanical and electrical sensitivity
25 of dual-axis gyroscopic sensor 300 may be calculated
according to the following equation:

$$\left|\frac{V_{out}}{\Omega_y}\right| = \left|\frac{\theta_x}{\Omega_y}\right|\left|\frac{V_{out}}{\theta_x}\right| = \left|\frac{2\theta_{z0}\omega_z}{\omega^2_x + \frac{j\omega_x\omega_z}{\Omega_x} - \omega^2_z}\right|\left|2\frac{\partial C}{\partial\theta_x}\frac{V_s}{C_I}\right| \qquad (19)$$

were V_s is the sense voltage, C_i is the capacitance of the
integrating capacitor, Q_x is the quality of inverse

- 44 -

damping coefficient, and V_{out} is the voltage signal from the mixer. One drawback of the sensing system is that a small inherent voltage is generated at twice the drive frequency. However, this voltage is far from the sense
5   modulation frequencies.

As described above, if dual-axis gyroscopic sensor 300 is rotating about an axis parallel to the surface of the substrate, then the oscillation of rotor 316 about the Z-axis induces an oscillation about the X-axis or Y-
10 axis due to the Coriolis force. In an ideal device, rotor 316 is perfectly aligned so that the only motion caused by drive system 310 is within the X-Y plane. However, fabrication imperfections may cause rotor 316 to wobble as it undergoes rotation about the Z-axis.
15 Specifically, even if the gyroscopic sensor 300 is not rotating about the X-axis or Y-axis, as rotor 316 rotates about the Z-axis, it may oscillate or wobble out of the X-Y plane. The wobble caused by the fabrication imperfections generates a false rotation rate measurement
20 called quadrature error. The quadrature error in dual-axis gyroscopic sensor 300 is similar to the quadrature error in Z-axis gyroscopic sensor 20; the quadrature error and Coriolis acceleration are both sinusoidal signals centered at the frequency of oscillation and
25 ninety degrees out of phase. Ideally, demodulation will eliminate the out-of-phase quadrature error. However, because the electronic components may have a small phase-lag, some percentage of the quadrature error will corrupt the measurement of the rotation rate.
30   Returning to FIG. 17A, quadrature correction system 314 includes eight correction electrodes 390a-390h. The correction electrodes are arranged in pairs with each outer comb 340a-340d surrounded by two opposing

- 45 -

correction electrodes. For example, outer comb 340a is flanked by correction electrodes 390a and 390b. Each correction electrode has a plurality of teeth 392 which are interdigitated with the teeth of the outer combs.

5 The quadrature correction system 314 may apply voltages to the correction electrodes 390a-390h in order to levitate teeth 344 of the outer combs and cancel the quadrature error.

Returning to FIG. 18, each pair of opposing

10 correction electrodes may be connected to a DC offset voltage source. In addition, the correction electrodes on opposite sides of the rotor may be connected. For example, correction electrode 390a may be electrically connected to correction electrode 390f. A first DC

15 voltage source 394 may connect electrode 390a to electrode 390b, and second DC voltage source 396 may connect correction electrode 390c and 390d. The DC offset may be selected to electrostatically levitate outer combs 340a-340d and thereby cancel the quadrature

20 error.

Referring to FIG. 19, a portion of substrate 304 beneath teeth 344 and 392 may be an n+ diffused region to provide a control pad electrode 398. The control pad electrode 398 is electrically connected to proof mass

25 302. By applying a generally positive voltage to teeth 392 and a generally negative voltage to teeth 344 and control pad electrode 398, the electric field (shown by field lines 399) generates an upward force F_z on teeth 344.

30 Returning to FIG. 17A, the correction electrodes 390a and 390f generate an upward force on the teeth on the left side of the rotor which is stronger than the upward force on the teeth on the right side of the rotor

- 46 -

generated by electrodes 390b and 390e. This force
imbalance creates a balancing torque which tends to
rotate the rotor so that, absent the Coriolis force, it
vibrates solely in the X-Y plane. Because the quadrature
5   error results in a linear displacement, the balancing
forces need to be proportional to the position of the
proof mass about the Z-axis. The balancing torque F_z is
proportional to the overlapping area between teeth 344
and teeth 392. Because the overlapping area between
10 teeth 344 and teeth 392 is directly proportional to the
angular position of rotor 316, the balancing torque will
also be proportional to the angular position of the
rotor.

       Referring to FIG. 20, another embodiment of dual-
15 axis gyroscopic sensor 300' includes a modified
quadrature correction system 314'. In quadrature
correction system 314', four generally rectangular or
wedge-shaped plates 340a'-340d' are connected to outer
edge 326 of rotor 316. Two fixed electrode pads 390a'
20 and 390b' are disposed on substrate 304 beneath each
plate. The fixed electrode pads 390a' and 390b' may be
formed of n+ diffused regions in the substrate. A DC
offset voltage may be applied between each pair of
electrode pads to correct the quadrature error. For
25 example, a positive offset voltage may be applied so that
the voltage of electrode pad 390b' is higher than the
voltage of electrode pad 390a'. As rotor 316 rotates
counter-clockwise and the plate 340a' moves rightwards,
more of the plate will overlap electrode pad 390b', and
30 thus the right side of the plate will be more attracted
to the substrate than the left side of the plate. This
will generate a torque which tends to rotate rotor 316
about the X-axis. The dual-axis gyroscopic sensor 300'

- 47 -

otherwise functions in a manner similar to dual-axis
gyroscopic sensor 300.

Referring to FIG. 21, in a gyroscopic sensor 400
the drive system, the sensing system, and the quadrature
5   correction system use a single set of electrodes.
Gyroscopic sensor 400 includes a proof mass 402 connected
to a substrate 404 by a flexible suspension 406. A
plurality of opposing electrode fingers 410a and 410b
(only two opposing fingers are shown) project from proof
10 mass 402 along the X-axis. Each electrode finger 410a is
flanked by respective stationary electrode fingers 412a
and 414a. Similarly, each electrode finger 410b is
flanked by stationary electrode fingers 412b and 414b.

To sense the position of the proof mass along the
15 Y-axis, a voltage source 420 applies a high-frequency
(e.g., one megahertz) AC voltage between upper electrode
fingers 412a, 412b and lower electrode fingers 414a,
414b. Proof mass 402 is electrically connected to an
integrator 422. The output of integrator 422 provides a
20 position signal.

To drive the proof mass along the X-axis, a
voltage-controlled oscillator 426 is connected to apply
an AC voltage with a frequency ω between the opposing
electrode fingers 412a, 414a and 412b, 414b. The output
25 of integrator 422 is applied to a phase-sensing circuit
428, and the output of phase-sensing circuit 428 controls
the voltage-controlled oscillator 426.

The output voltage V_{out} from integrator 422 is

$$V_{out} = \frac{Q_{struct}}{C_I} \qquad\qquad (20)$$

- 48 -

where Q_{struct} is the charge on the proof mass and C_I is the capacitance of integrator 422. Q_{struct} is given by the equation:

$$Q_{struct} = \frac{dC_s}{dy}\Delta y V_{sense} + \Delta C_x(t) V_F(t) \tag{21}$$

where $V_F(t)$ is AC portion of the forcing voltage, $C_x(t)$ is
5 the changing capacitance on the forcing electrodes as the structure displaces along the X-axis, and V_{sense} is the sense voltage applied by voltage source 420. Combining Equations 20 and 21 yields:

$$V_{out} = \frac{\Delta C_x(t) V_F(t)}{C_I} + other\ terms \tag{22}$$

If the forcing voltage $V_F(t)$ is $V_F\sin(\omega t)$ then the
10 resulting displacement $x(t)$ is given by the following equation:

$$x(t) = X_0(\omega, \omega_x)\sin(\omega t + \phi(\omega, \omega_x)) \tag{23}$$

where ω is the drive frequency, ω_x is the driven mode resonance frequency, $X_0(\omega, \omega_x)$ is the amplitude, and $\phi(\omega, \omega_x)$ is a phase difference. Because $\Delta Cx(t)$ is
15 proportional to $x(t)$,

$$V_{out} = \frac{\Delta C_x(\omega, \omega_x)}{C_I}\sin(\omega t + \phi(\omega, \omega_x))\sin(\omega t) \tag{24}$$

and therefore

$$V_{out} = \frac{\Delta C_x(\omega, \omega_x)}{2C_I}[\cos(\phi(\omega, \omega_x)) - \cos(2\omega t + \phi(\omega, \omega_x))] \tag{25}$$

When the drive frequency ω is equal to the resonant frequency ω_x, the phase ϕ will be 90°. Because

- 49 -

the $\cos(\phi(\omega,\omega_x))$ term of Equation 25 produces a DC offset, phase-sensing circuit 428 can drive the frequency ω of voltage-controlled oscillator 426 to the resonant frequency ω_x by sensing when there is no DC offset. Thus,

5 the drive voltage will remain phase locked with the position of the proof mass.

Quadrature error correction may be accomplished in gyroscopic sensor 400 by applying a DC voltage between electrode fingers 412a and 414a and an equal but opposite

10 DC voltage between electrode fingers 412b and 414b.

Referring to FIG. 22, a micromachined gyroscopic sensor 500 may be fabricated using high-aspect-ratio single-crystal-silicon micromachining techniques to produce an extremely thick device. Gyroscopic sensor 500

15 includes a vibratory structure 502 connected to a rigid frame or substrate 504 at anchor points 511. Structure 502 is configured to vibrate in a plane parallel to a surface 505 of the substrate. As such, a gap of about 0.5 to 4.0 microns, such as about 1.0 microns, separates

20 the vibratory structure from surface 505.

Structure 502 is generally H-shaped, and includes a proof mass portion 506 and a flexible suspension portion 508. The suspension portion includes two parallel crossbeams 516 and four parallel flexures 510

25 positioned generally along the X-axis. One end of each flexure is connected to anchor 511 which connects structure 502 to the substrate, and the other end of each flexure is connected to one of crossbeams 516. The total length of one crossbeam 516 and two flexures 510 may be

30 about 200 to 1500 microns in length, preferably about 1250 microns.

Proof mass portion 506 includes two crossbars 512 connected to two beams 514 to provide a generally square

- 50 -

arrangement. Three additional crossbars 512 are also
connected between beams 514. A plurality of electrode
teeth or fingers project along the X-axis from the
crossbars 512. Four additional flexures 518 may connect
5 flexures 510 to proof mass portion 506.

Structure 502 may be formed of single-crystal
silicon. The structure 502 may have a thickness T of at
least 25 microns, and it is advantageous for the
thickness T to be at least 50 microns. The thickness may
10 be between about 50 and 100 microns, but for some
applications the thickness may be 250 microns. The
flexures of the structure may have a width W_F of about two
to five microns. The aspect ratio, i.e., the ratio of
width to thickness, of the flexures should be greater
15 than 10:1, and it is advantageous for the aspect ratio to
be greater than 20:1. The aspect ratio may even be 50:1
or more. The beams and crossbars of the proof mass
portion may have a width W_B of about five to ten microns.
The total mass of structure 502 may be about 10 to 50
20 micrograms.

The suspension portion 508 is designed to be
flexible along the X-axis and Y-axis and rigid to other
modes of vibration. In particular, the high-aspect ratio
of the flexures results in a structure which is very
25 rigid to torsion and Z-axis acceleration.

Referring to FIG. 23, the micromachined gyroscopic
sensor 500 includes four major electronic elements: a
drive system 520 used to sustain oscillation of structure
502 along the X-axis, a sensing system 540 used both to
30 detect deflections of structure 502 along the Y-axis, a
sense tuning system 560 used to adjust the resonant
frequency of structure 502 along the Y-axis, and a

quadrature correction system 580 used to apply electrostatic forces to cancel quadrature error.

As shown in FIGS. 15 and 16, the drive system 520 includes two opposing driving electrode combs 522a and 5 522b and two feedback electrode combs 524a and 524b, all connected to substrate 504. Each driving electrode comb and feedback electrode comb includes a plurality of electrode teeth or fingers 526 which project along the drive axis and which are interdigited with electrode 10 teeth or fingers 528 which project from structure 502. Electrode teeth 526 and 528 may have a length L of about fifteen microns, and a width W_E of about two to six microns. Electrode teeth 526 may be separated from electrode teeth 528 by a gap of about 2.5 microns. 15 Electrode teeth 526 and 528 may be formed from the same layer of single-crystal silicon and have a thickness of about 100 microns.

The feedback electrodes combs 524a and 524b are electrically connected to the positive and negative 20 inputs of a trans-resistance amplifier 530. The driving electrode combs 522a and 522b are connected to the positive and negative outputs, respectively, of the transresistance amplifier and to a phase-locked loop circuit 532. At least one of the outputs from 25 transresistance amplifier 530 may be mixed with a velocity signal from phase-locked loop 532 by a mixer 534. The output of mixer 534 is then used to modulate transresistance amplifier 530 to provide an automatic gain control circuit to control the oscillation amplitude 30 of structure 502.

The sensing system 540 includes an opposing pair of sense electrode combs, including left sense electrode combs 542a and 542b, and right sense electrode combs 544a

- 52 -

and 544b. The left sense electrode combs 542a, 542b
include a plurality of "left" electrode teeth 546, and
the right sense electrode combs 544a, 544b include a
plurality of "right" electrode teeth 548. The electrode
5   teeth 546 and 548 are interdigited with electrode teeth
550 which project from structure 502 such that each
electrode tooth 550 is disposed between one left tooth
546 and one right tooth 548.

      Electrode teeth 546, 548 and 550 may have a length
10 L of about fifteen microns, and width W_F of about two to
six microns. Electrode teeth 546, 548 and 550 have a
thickness of at least 25 microns, and the thickness may
be between about 50 and 100 microns. The aspect ratio of
the electrode teeth should be at least about 5:1. The
15 aspect ratio may be at least 10:1, and it may be between
about 10:1 and 20:1. Electrode teeth 550 may be
separated from electrode teeth 546 and 548 by a gap
having a width W_G between about 0.5 and 4.0 microns, such
as 2.5 microns. The aspect ratio of the gap should be at
20 least 10:1, and it may be greater than 20:1 or even
greater than 50:1. Electrode teeth 546, 548 and 550 may
be formed from the same layer of single-crystal silicon
in the same fabrication step so that the teeth are
coplanar.
25   A first sense voltage source 552 applies an AC
voltage to left sense electrode combs 542a and 542b. A
second sense voltage source 554 applies an AC voltage,
180° out of phase with the first sense voltage, to right
sense electrode combs 544a and 544b. The sense voltage
30 sources may generate AC signals having a maximum voltage
of about 0.1 to 5.0 volts and a frequency of about 0.1 to
5.0 megahertz. The AC signals may have a voltage
amplitude of one volt and a frequency of one megahertz.

- 53 -

To measure the Coriolis signal Ω_z, structure 502 is electrically connected to an integrator 556, and the output of integrator 556 is amplified by an AC amplifier 558. The signal from one of the sense voltage sources is
5 mixed with a position signal from phase-locked loop 532 by a mixer 536. The output of mixer 536 is then mixed with the output of amplifier 558 by a mixer 538 to generate the Coriolis signal.

Tuning of the Y-axis resonant frequency may be
10 accomplished sense tuning system 560 applying a DC bias voltage between a set of inner tuning electrodes 562 and outer tuning electrodes 564. Electrodes 566 project from structure 502 and are interdigited with the inner tuning electrodes 562 and outer tuning electrodes 564. A tuning
15 voltage source 568 applies a bias voltage $V_{\Delta fy}$ between inner tuning electrodes 562 and outer tuning electrodes 564. Alternately, the Y-axis resonant frequency could be tuned by applying a DC bias between the vibratory structure and the tuning electrodes.

20   Quadrature error cancellation is accomplished by applying a voltage between diagonal pairs of electrodes. The quadrature error correction system 580 includes a lower left electrode 582a, an upper left electrode 582b, a lower right electrode 584a, and an upper right
25 electrode 584b. Lower left electrode 582a is connected to upper right electrode 584b, and upper left electrode 582b is connected to lower right electrode 584a. A quadrature correction voltage source 586 applies a bias voltage $2V_{Quad}$ between the electrode pairs 582a, 584b and
30 582b, 584a. The bias voltage creates a balancing force which is proportional to the position of the proof mass along the X-axis. This bias voltage may be determined

- 54 -

experimentally (as shown in FIG. 13) and may be in the
range of 1 mV to 100 mV.

In addition, quadrature error correction system
580 may include a feedback loop to automatically adjust
5   the bias voltage. A velocity signal from phase-locked
loop 532 may be mixed with a signal from one of the sense
voltage sources by a mixer 590. The output of mixer 590
may be mixed with the output of amplifier 558 by a mixer
592. The output of mixer 592 may be used to control the
10 voltage source 586.

Assuming that the mass M of structure 502 is 36
micrograms, the drive and sense frequencies ω_x and ω_y are
each 63 kHz, the quality factor Q for single-crystal
silicon is 200,000 (about three to four times higher than
15 that of polysilicon), and the amplitude X_0 of the drive
mode is five microns, then one may calculate from
Equation 16 that, at room temperature, the Brownian noise
Ω_{nB} for a bandwidth (BW) of 60 Hz is about 2 deg/hr.

The electronic noise floor is determined by the
20 thermal noise level in charge integrator 556. Where the
sense frequency ω_y is electrostatically tuned to the drive
frequency ω_x plus an offset frequency $\Delta\omega$, the electronic
noise Ω_{nE} may be calculated from the equation:

$$\Omega_{nE} = 2\frac{g_0 \Delta\omega}{X_0 V_s}\sqrt{\frac{32}{3\pi}(\frac{k_B T}{C_s})\frac{1}{f_T}((1+\frac{C_P}{C_s})BW} \tag{26}$$

where g_0 is the sense-capacitor gap width, X_0 is the
25 oscillation amplitude, V_s is the sense voltage, k_B is
Boltzmann's constant, T is the temperature, C_s is the
sense capacitance, C_P is the parasitic capacitance, f_T is
the CMOS transition frequency, and BW is the bandwidth.

- 55 -

Assuming that the sense-capacitor gap g_0 is 2.5 microns, the sense voltage V_s is 1 V, C_s is the sense capacitance C_s is 1.25 pF, the parasitic capacitance C_p is 0.25 pF, and the CMOS transition frequency f_T is 1 GHz,

5 one may calculate from Equation 18 that a frequency offset $\Delta\omega$ of $2\pi(175\ Hz)$ is required to make the electronic noise floor equal to 2.5 deg/hr. This degree of tuning is feasible in principle because the measurement bandwidth is about 60 Hz.

10 By increasing the thickness of electrode teeth 546, 548 and 550, the surface area between the stationary and movable electrodes is increased, resulting in a larger sense capacitance. The larger sense capacitance reduces electronic noise. Similarly, the thicker

15 structure is more massive and thus less subject to Brownian motion. In short, a gyroscopic sensor using high-aspect-ratio single-crystal silicon structures may be about one-hundred times more sensitive than a gyroscopic sensor using structures formed of thin

20 polysilicon layers.

Fabrication of gyroscopic sensor 500 includes six basic steps: handle wafer processing, device wafer processing, bonding, CMOS processing of the bonded structure, etching to form the vibratory structure and

25 stationary electrodes, and capping.

Referring to FIG. 24A, processing of a bottom substrate 600 may begin with a handle wafer 602, which may be a single-crystalline silicon substrate. Handle wafer 602 is oxidized to form an oxide layer 604, and a

30 polysilicon layer 606 is deposited on oxide layer 604. Polysilicon layer 606 is then doped, polished and patterned to form the interconnects for the electrically isolated electrodes 522a, 522b, 524a, 524b, 542a, 542b,

- 56 -

544a, 544b, 562, 564, 582a and 584b, and 582b and 584a, of the gyroscopic sensor.

   Referring to FIG. 24B, processing of a top substrate 610 may begin with a device wafer such as a
5 silicon-on-insulator (SOI) substrate. The device wafer includes an oxide layer 616 sandwiched between two single-crystal silicon layers 614 and 618. A shallow trench 620 is formed in a surface 622 of single-crystal silicon layer, except in regions 624. Regions 624 will
10 form anchors 511 connecting vibratory structure 502 to substrate 504. Trench 620 may be formed by deposition of a photoresist mask, etching of the exposed portions of single-crystal silicon layer 614, and removal of the mask. Alternately, trench 620 may be formed by
15 mechanical thinning.

   The thickness of single-crystal silicon layer 614 will define the thickness of vibratory structure 502, and the depth of trench 620 will define the spacing between the vibratory structure and the substrate. Preferably,
20 single-crystal silicon layer 614 is about 100 microns thick, and trench 620 is about one micron deep.

   Referring to FIG. 24C, bottom substrate 600 and top substrate 610 are aligned with surface 622 of top substrate 610 abutting the patterned polysilicon layer
25 606 of bottom substrate 600. The top and bottom substrates are bonded so that trench 620 forms a sealed cavity 626 between the two substrates. Then, referring to FIG. 24D, top substrate 610 is thinned by etching or mechanical removal of single-crystal silicon layer 618 to
30 expose oxide layer 616, and oxide layer 616 is stripped. At this point, the bonded assembly is ready for standard CMOS processing. Because sealed cavity 626 is completely internal, the bonded assembly appears as an unprocessed

- 57 -

silicon wafer and may processed with conventional
techniques.

Referring to FIG. 24E, the integrated circuitry of
gyroscopic sensor 500 is fabricated on an exposed surface
5 630 of single-crystal silicon layer 614 in device regions
632. Following circuit fabrication, a thermocompression
bond layer 634 is deposited and patterned. The bond
layer 634 may be a conductive metal, such as gold.

Referring to FIG. 24F, the structures of the
10 gyroscopic sensor are formed in single-crystal silicon
layer 614.   A photoresist mask is deposited over bond
layer 634 and exposed surface 630, and the photoresist
mask is patterned to define the gaps between the
vibratory structure 502 and the stationary electrodes
15 (not shown in this cross-sectional view). The single-
crystal silicon layer 614 is etched using inductively-
coupled plasma based deep reactive ion etching until
cavity 626 is exposed. The etching step forms trenches
636 which create the free-standing vibratory structure
20 and the various electrode structures of the gyroscopic
sensor. Following the reactive ion etching, an oxygen
plasma may be used to remove the photoresist mask, and
the assembly may undergo a UV-ozone clean.

Finally, referring to FIG. 24G, a capping wafer
25 640 is aligned and bonded to top substrate 610. Capping
wafer 640 may be glass or oxidized silicon. An underside
642 of the capping wafer may include a patterned
thermocompression bond layer 644.   Bond layer 634 may be
aligned with bond layer 644, and the thermocompression
30 bond may be formed by the application of a pressure of
approximately 20 psi and a temperature of about 300-350°C
for several minutes. The capping wafer may also include

- 58 -

an etched hole 646 that permits access to bonding pads 648 in device regions 632.

The present invention has been described in terms of a preferred embodiment. The invention, however, is
5 not limited to the embodiment depicted and described. Rather, the scope of the invention is defined by the appended claims.

What is claimed is:

- 59 -

1.   A microfabricated structure comprising:
       a substrate;
       a mass connected to said substrate by a suspension
system to vibrate in a plane parallel to a surface of
5 said substrate;
       a first plurality of electrode fingers projecting
from said mass along a first axis in said plane;
       a second plurality of electrode fingers, coplanar
with said first plurality of electrode fingers, connected
10 to said substrate and projecting substantially along said
first axis;
       a third plurality of electrode fingers connected
to said substrate but electrically isolated from said
second plurality of electrode fingers, said first third
15 plurality of electrode fingers being coplanar with said
first and second plurality of electrode fingers and
projecting substantially along said first axis, said
second and third plurality of electrode fingers
interdigitated with said first plurality of electrode
20 fingers such that each of said first plurality of
electrode fingers is adjacent to one of said second
plurality of electrode fingers and one of said third
plurality of electrode fingers.

2.   The structure of claim 1 further comprising a
25 voltage source to apply a voltage between said second and
third plurality of electrode fingers.

3.   The structure of claim 1 further comprising
       a fourth plurality of electrode fingers, coplanar
with said first, second and third plurality of electrode

- 60 -

fingers, projecting from said mass along said first axis, and

a fifth plurality of electrode fingers connected to said substrate but electrically isolated from said
5 second and third plurality of electrode fingers, said fourth and fifth plurality of electrode fingers interdigitated.

4. The structure of claim 3 wherein each of said first plurality of electrode fingers has a first length
10 and each of said fourth plurality of electrode fingers has a second length.

5. The structure of claim 4 wherein said first length is greater than said second length.

6. A microfabricated structure comprising:
15 a substrate; and

a suspension system to permit a mass to vibrate in a plane parallel to a surface of said substrate, said suspension system including,

first and second substantially parallel
20 beams, each of said first and second beams anchored at both ends to said substrate, and

third and fourth substantially parallel beams, one end of each of said third and fourth beams connected to said first beam and another end connected to
25 said second beam.

7. The structure of claim 6 further comprising a plurality of fingers projecting along an axis substantially parallel to said first and second beams.

- 61 -

8.   The structure of claim 6 further comprising

        a fifth and a sixth beam, one end of each of said
fifth beam and sixth beams connected to said third beam
and another end connected to said fourth beam, and

5   a seventh beam, one end of said seventh beam
connected to said fifth beam and another end connected to
said sixth beam.

9.   The structure of claim 8 further comprising a
plurality of fingers projecting from said seventh beam
10 along an axis substantially parallel to said first and
second beams.

10.   The structure of claim 6 wherein sections of said
first and second beams located between said third and
fourth beams are substantially rigid to prevent rotation
15 of said mass.

11.   A sensor comprising:
        a substrate;
        a mass connected to said substrate by a suspension
system to vibrate in a plane parallel to a surface of
20 said substrate;
        a first plurality of electrode fingers projecting
from said mass along a first axis in said plane;
        a second plurality of electrode fingers connected
to said substrate and projecting substantially along said
25 first axis;
        a third plurality of electrode fingers connected
to said substrate but electrically isolated from said
second plurality of electrode fingers, said third
plurality of electrode fingers projecting substantially
30 along said first axis, said second and third pluralities

- 62 -

of electrode fingers interdigitated with said first plurality of electrode fingers such that each of said first plurality of electrode fingers is adjacent to one of said second plurality of electrode fingers and one of
5   said third plurality of electrode fingers;

a position sensor to mesure a deflection of said mass in said plane; and

a voltage source for applying a first DC voltage between said second and third pluralities of electrode
10   fingers to cause said mass to vibrate, absent a Coriolis force, more precisely along said first axis.

12.   The sensor of claim 11 further including,

a fourth plurality of electrode fingers projecting from said mass along a first axis in said plane and
15   positioned opposing said first plurality of electrode fingers;

a fifth plurality of electrode fingers connected to said substrate and projecting substantially along said first axis;

20   a sixth plurality of electrode fingers connected to said substrate but electrically isolated from said fifth plurality of electrode fingers, said sixth plurality of electrode fingers projecting substantially along said first axis, said fifth and sixth plurality of
25   electrode fingers interdigitated with said third plurality of electrode fingers such that each of said fourth plurality of electrode fingers is adjacent to one of said fifth plurality of electrode fingers and one of said sixth plurality of electrode fingers.

30   13.   The sensor of claim 12 further comprising a second voltage source for applying a second DC voltage between

- 63 -

said fifth and sixth plurality of electrode fingers to cause said mass to vibrate, absent a Coriolis force, more precisely along said first axis.

14.   The sensor of claim 13 wherein said second DC
5 voltage is substantially equal in magnitude but opposite in sign to said first DC voltage.

15.   The sensor of claim 13 wherein said first plurality of electrode fingers is electrically coupled to said second plurality of electrode fingers.

10 16.   The sensor of claim 13 further comprising a voltage source for applying a third DC voltage between said first and third pluralities of electrode fingers and said second, third, fifth and sixth pluralities of electrode fingers to adjust the resonant frequency of
15 vibrations of said mass along a second axis in said plane perpendicular to said first axis.

17. The sensor of claim 11 wherein the position sensor measures the deflection of said mass along a second axis substantially perpendicular to said first axis and
20 rotation of said mass about a Z-axis perpendicular to said surface and vibration of said mass along said first axis generates a Coriolis force to deflect said mass along said second axis, and wherein the sensor further comprises a signal processor coupled to an output of
25 said position sensor to generate a signal varying with the rate of rotation of said mass about the Z-axis.

- 64 -

18.   The sensor of claim 17 further comprising a
voltage source for applying an AC voltage between said
second and third plurality of electrode fingers.

19.   The sensor of claim 18 wherein a voltage is
5   applied between said second and third pluralities of
electrode fingers to form a capacitive bridge with said
first plurality of electrodes, and said position sensor
is coupled to said first plurality of electrodes to
detect changes in capacitance when said mass is deflected
10 along said second axis.

20.   A sensor comprising:
        a substrate;
        a mass connected to said substrate by a suspension
system to vibrate in a plane parallel to a surface of
15 said substrate;
        a first plurality of electrode fingers projecting
from said mass along a first axis in said plane;
        a second plurality of electrode fingers connected
to said substrate and projecting substantially along said
20 first axis;
        a third plurality of electrode fingers connected
to said substrate but electrically isolated from said
second plurality of electrode fingers, said first third
plurality of electrode fingers projecting substantially
25 along said first axis, said second and third plurality of
electrode fingers interdigitated with said first
plurality of electrode fingers such that each of said
first plurality of electrode fingers is adjacent to one
of said second plurality of electrode fingers and one of
30 said third plurality of electrode fingers; and

a voltage source for applying a DC voltage between
said first plurality of electrode fingers and said second
and third plurality of electrode fingers to adjust the
resonant frequency of vibrations of said mass along a
5 second axis in said plane perpendicular to said first
axis.

21.   A microfabricated gyroscopic sensor for sensing
rotation about a Z-axis, comprising:
        a substrate;
10   a mass connected to said substrate by a suspension
system to vibrate in a plane parallel to a surface of
said substrate;
        a drive system to cause said mass to vibrate
substantially along a first axis in said plane;
15   a first plurality of electrode fingers projecting
from said mass substantially along said first axis;
        a second plurality of electrode fingers connected
to said substrate and projecting substantially along said
first axis;
20   a third plurality of electrode fingers connected
to said substrate and projecting substantially along said .
first axis, said second and third plurality of electrode
fingers interdigitated with said first plurality of
electrode fingers such that each of said first plurality
25 of electrode fingers is adjacent to one of said second
plurality of electrode fingers and one of said third
plurality of electrode fingers;
        a position sensor coupled to said first plurality
of electrode fingers for measuring the deflection of said
30 mass along a second axis in said plane perpendicular to
said first axis, wherein rotation of said mass about a Z-
axis perpendicular to said surface and vibration of said

mass along said first axis generates a Coriolis force to deflect said mass along said second axis; and

a signal processor coupled to an output of said position sensor to generate a signal varying with the
5   rate of rotation of said mass about the Z-axis.

22.   The sensor of claim 21 further comprising a voltage source for applying an AC voltage having a first frequency between said second and third plurality of electrode fingers.

10 23.   The sensor of claim 22 wherein a voltage is applied between said second and third pluralities of electrode fingers to form a capacitive bridge with said first plurality of electrodes, and said position sensor is coupled to said first plurality of electrodes to
15 detect changes in capacitance when said mass is deflected along said second axis.

24.   The sensor of claim 23 wherein said position sensor further includes an integrator to integrate a signal from said first plurality of electrode fingers.

20 25.   The sensor of claim 24 wherein said drive system generates a signal to cause said mass to oscillate along said first axis at a second frequency.

26.   The sensor of claim 25 wherein said drive system said signal.

25 27.   The sensor of claim 25 further including a first mixer to mix the signal from said drive system with a signal from said voltage source.

- 67 -

28.   The sensor of claim 27 further including a second
mixer to mix a signal from said first mixer with an
output signal from said position sensor to produce a
position quadrature signal.

5 29.   The sensor of claim 27 further including a second
mixer to mix a signal from said first mixer with an
output signal from said position sensor to produce a
Coriolis signal.

30.   The sensor of claim 25 further including a mixer
10 to mix an output signal from said position sensor with a
signal from said voltage source to produce a position
signal.

31.   A microfabricated gyroscopic sensor, comprising:
15   a substrate;
         a mass connected to the substrate by a suspension
system;
         a drive system to cause the mass to vibrate along
a drive axis substantially parallel to a surface of the
20 substrate; and
         a position sensor to measure a deflection of the
mass along a sense axis substantially parallel to the
surface of the substrate, wherein rotation of the mass
about an axis of rotation substantially perpendicular to
25 the surface of the substrate and vibration of the mass
along the drive axis generates a Coriolis force to
deflect the mass along the sense axis.

32.   The sensor of claim 31 further comprising a
processor coupled to an output of the position sensor to

- 68 -

generate a signal varying with the rate of rotation of
the mass about the axis of rotation.

33.   The sensor of claim 31 wherein the position sensor
includes a first sense electrode projecting from the
5 mass, a second sense electrode connected to the substrate
and positioned on a first side of the first electrode,
and a third sense electrode connected to the substrate
and positioned on an opposing second side of the first
electrode.

10 34.   The sensor of claim 33 wherein the position sensor
senses a change in capacitance between the first
electrode and the second and third electrodes.

35.   The sensor of claim 33 wherein the first, second
and third electrodes are substantially coplanar and each
15 electrode has a longitudinal axis substantially aligned
with the drive axis.

36.   The sensor of claim 31 wherein the drive system
includes a first drive electrode projecting from the
mass, a second drive electrode connected to the substrate
20 and positioned on a first side of the first electrode,
and a third drive electrode connected to the substrate
and positioned on an opposing second side of the first
electrode.

37.   The sensor of claim 35 wherein the drive system
25 applies an alternating voltage between the between the
first electrode and the second and third electrodes.

38.   The sensor of claim 33 wherein the first, second and third electrodes are substantially coplanar and each electrode has a longitudinal axis substantially aligned with the drive axis.

5   39.   The sensor of claim 31 further comprising a voltage source to apply a voltage between a plurality of correction electrodes connected to the substrate to cause the mass to vibrate, absent the Coriolis force, more precisely along the drive axis.

10 40.   The sensor of claim 31 further comprising a voltage source to apply a voltage between a first tuning electrode connected to the substrate and a second tuning electrode connected to the mass to adjust a resonant frequency of vibrations of the mass along the sense axis.

15 41.   A microfabricated gyroscopic sensor, comprising:
            a substrate;
            a mass connected to the substrate by a suspension system;
            a drive system to cause the mass to vibrate
20 substantially along a drive axis;
            a position sensor to measure a deflection of the mass along a sense axis, wherein rotation of the mass about an axis of rotation and vibration of the mass along the drive axis generates a Coriolis force to deflect the
25 mass along the sense axis; and
            a voltage source to apply a voltage between electrodes connected to the substrate to cause the mass to vibrate, absent the Coriolis force, more precisely along the drive axis.

- 70 -

42.   The sensor of claim 41 further comprising a
processor coupled to an output of the position sensor to
generate a signal varying with the rate of rotation of
the mass about the axis of rotation.

5   43.   The sensor of claim 41 further comprising   a
second voltage source to apply a second voltage between
electrodes connected to the mass and the electrodes
connected to the substrate to adjust a resonant frequency
of vibrations of the mass along the sense axis.

10 44.   The sensor of claim 41 wherein the position sensor
applies an AC voltage between the electrodes connected to
the substrate.

45.   The sensor of claim 41 wherein the drive axis and
sense axis are substantially parallel to a surface of the
15 substrate and the axis of rotation is substantially
perpendicular to the surface of the substrate.

46.   The sensor of claim 41 further comprising:
         a first plurality of electrode fingers projecting
from the mass substantially along the drive axis;
20   a second plurality of electrode fingers connected
to the substrate and projecting substantially along the
drive axis; and
         a third plurality of electrode fingers connected
to the substrate and projecting substantially along the
25 drive axis, the second and third pluralities of electrode
fingers interdigitated with the first plurality of
electrode fingers such that each of the first plurality
of electrode fingers is adjacent to one of the second

plurality of electrode fingers and one of the third
plurality of electrode fingers.

47.   The sensor of claim 46 further comprising:
       a fourth plurality of electrode fingers projecting
5 from the mass substantially along the drive axis and
positioned opposing the first plurality of electrode
fingers;
       a fifth plurality of electrode fingers connected
to the substrate and projecting substantially along the
10 drive axis and positioned opposing the second plurality
of electrode fingers; and
       a sixth plurality of electrode fingers connected
to the substrate and projecting substantially along the
drive axis and positioned opposing the third plurality of
15 electrode fingers, the fifth and sixth pluralities of
electrode fingers interdigitated with the fourth
plurality of electrode fingers such that each of the
fourth plurality of electrode fingers is adjacent to one
of the fifth plurality of electrode fingers and one of
20 the sixth plurality of electrode fingers.

48.   The sensor of claim 47 wherein the first, second,
third, fourth, fifth and sixth pluralities of electrode
fingers are substantially co-planar.

49.   The sensor of claim 48 wherein the voltage source
25 applies a first DC voltage between the second plurality
and the third plurality of electrode fingers and a second
DC voltage between the fifth plurality and the sixth
plurality of electrode fingers.

- 72 -

50.   The sensor of claim 49 wherein the second DC voltage is substantially equal in magnitude and opposite in sign to the first DC voltage.

51.   The sensor of claim 21 further comprising   a
5 voltage source for applying a DC voltage between the first plurality of electrode fingers and the second and third pluralities of electrode fingers to adjust a resonant frequency of vibrations of the mass along the second axis.

10 52.   The sensor of claim 21 further comprising a voltage source for applying a first DC voltage between the second and third pluralities of electrode fingers to cause the mass to vibrate, absent a Coriolis force, more precisely along the first axis.

15 53.   A method of sensing rotation with a gyroscopic sensor including a mass connected to a substrate by a suspension system, comprising:
        rotating the mass about an axis of rotation substantially perpendicular to a surface of the
20 substrate;
        causing the mass to vibrate substantially along a drive axis substantially parallel to the surface of the substrate, rotation of the mass about the axis of rotation and vibration of the mass along the drive axis
25 generating a Coriolis force to deflect the mass along a sense axis substantially parallel to the surface of the substrate; and
        measuring a deflection of the mass along the sense axis.

- 73 -

54.   A method of sensing rotation with a gyroscopic
sensor including a mass connected to a substrate by a
suspension system, comprising:
        rotating the mass about an axis of rotation;
5   causing the mass to vibrate substantially along a
drive axis, rotation of the mass about the axis of
rotation and vibration of the mass along the drive axis
generating a Coriolis force to deflect the mass along a
sense axis;
10   measuring a deflection of the mass along the sense
axis; and
        applying a voltage between electrode fingers
connected to the substrate to cause the mass to vibrate,
absent a Coriolis force, more precisely along the first
15 axis.

55.   A microfabricated gyroscopic sensor for measuring
rotation about an input axis, comprising:
        a substrate;
        a mass;
20   a suspension system connecting the mass to the
substrate;
        a drive system to cause the mass to oscillate
substantially about a drive axis;
        a position sensor to measure a rotation of the
25 mass about a sense axis, wherein rotation of the mass
about the input axis and oscillation of the mass about
the drive axis generates a Coriolis force to oscillate
the mass about the sense axis;
        a plurality of electrodes associated with the
30 substrate; and

- 74 -

a voltage source to apply a voltage between the
electrodes to cause the mass to oscillate, in the absence
the Coriolis force, more precisely about the drive axis.

56.   The sensor of claim 55 further comprising a
5 processor coupled to an output of the position sensor to
generate a signal varying with the rate of rotation of
the mass about the input axis.

57.   The sensor of claim 55 further comprising a second
voltage source to apply a second voltage between
10 electrodes connected to the mass and the electrodes
connected to the substrate to adjust a resonant frequency
of oscillations of the mass about the sense axis.

58.   The sensor of claim 55 wherein the position sensor
applies an AC voltage between the electrodes connected to
15 the substrate.

59.   The sensor of claim 55 wherein the drive axis is
substantially perpendicular to the surface of the
substrate and the input axis and sense axis are
substantially parallel to a surface of the substrate.

20 60.   The sensor of claim 59 further comprising:
a first plurality of electrode fingers projecting
from the mass;
a second plurality of electrode fingers projecting
from the mass;
25   a third plurality of electrode fingers projecting
from the substrate and interdigitated with the first
plurality of electrode fingers; and

a fourth plurality of electrode fingers projecting
from the substrate and positioned opposing the first
plurality of electrode fingers, the fourth plurality of
electrode fingers interdigitated with the second
5   plurality of electrode fingers.

61.   The sensor of claim 60 further comprising:
a fifth plurality of electrode fingers projecting
from the mass;
a sixth plurality of electrode fingers projecting
10 from the mass;
a seventh plurality of electrode fingers
projecting from the substrate and interdigitated with the
fifth plurality of electrode fingers; and
a eighth plurality of electrode fingers projecting
15 from the substrate and positioned opposing the seventh
plurality of electrode fingers, the eighth plurality of
electrode fingers interdigitated with the sixth plurality
of electrode fingers.

62.   The sensor of claim 61 wherein the first, second,
20 third, fourth, fifth, sixth, seventh and eighth
pluralities of electrode fingers are substantially co-
planar.

63.   The sensor of claim 62 wherein the voltage source
applies a first DC voltage between the third plurality
25 and the fourth plurality of electrode fingers and a
second DC voltage between the seventh plurality and the
eighth plurality of electrode fingers.

64.   The sensor of claim 63 wherein the second DC
voltage is substantially equal in magnitude and opposite
in sign to the first DC voltage.

65.   The sensor of claim 55 further comprising a first
5   electrode projecting from the mass, a second electrode
connected to the substrate and positioned beneath a first
portion of the first electrode, and a third electrode
connected to the substrate and positioned beneath a
second portion of the first electrode.

10 66.   The sensor of claim 55 wherein the mass is
substantially ring-shaped.

67.   A method of sensing rotation with a gyroscopic
sensor including a mass connected to a substrate by a
suspension system, comprising:
15   rotating the mass about an input axis;
            causing the mass to oscillate substantially about
a drive axis, rotation of the mass about the input axis
and oscillation of the mass about the drive axis
generating a Coriolis force to oscillate the mass about a
20 sense axis;
            measuring an oscillation of the mass about the
sense axis; and
            applying a voltage between electrodes connected to
the substrate to cause the mass to oscillate, in the
25 absence of a Coriolis force, more precisely about the
drive axis.

68.   A microfabricated gyroscopic sensor, comprising:
            a substrate having a first plurality of electrode
teeth;

a vibratory structure including a second plurality
of electrode teeth and a suspension system connecting the
second plurality of electrode teeth to the substrate, the
second plurality of electrode teeth interdigited with the
5   first plurality of electrode teeth;

a drive system to cause the vibratory structure to
oscillate relative to the substrate; and

a position sensor to measure a deflection of the
mass caused by a Coriolis force;

10   wherein the first and second pluralities of
electrode teeth have thicknesses substantially greater
than their widths.

69.   The sensor of claim 68 wherein the suspension
system includes a plurality of flexures having an aspect
15   ratio of at least about 10:1.

70.   The sensor of claim 68 wherein the first and
second pluralities of electrode teeth have an aspect
ratio of at least 5:1.

20   71.   The sensor of claim 68 wherein gaps between the
first and second pluralities of electrode teeth have an
aspect ratio of at least 10:1.

72.   A method of fabricating a gyroscopic sensor,
comprising:
25   forming an insulative layer on a first substrate;
forming a recess in a first surface of a second
substrate;

bonding the first surface of the second substrate
to the first substrate so that the recess defines an
30   enclosed cavity between the first and second substrates;

- 78 -

forming circuitry for the gyroscopic sensor on a
second surface of the second substrate

etching a plurality of trenches in the second
substrate from the second surface to the cavity, the
5 plurality of trenches defining a vibratory structure
connected to the first substrate.

73.   The method of claim 72 wherein the vibratory
structure has a thickness of at least 25 microns.

74.   The method of claim 72 wherein the recess has a
10 depth of about 1 micron.

75.   The method of claim 72 wherein the etching step
comprises a deep reactive ion etch.

FIG._1

2 / 22

FIG.__2

FIG._3

4 / 22
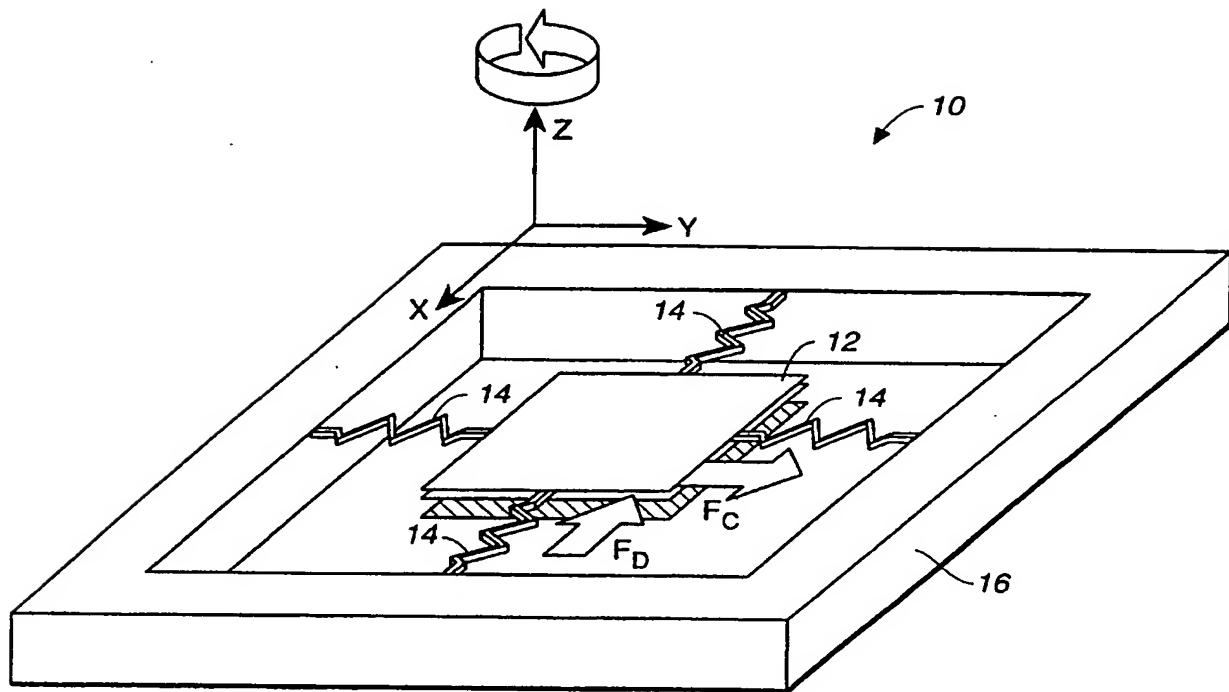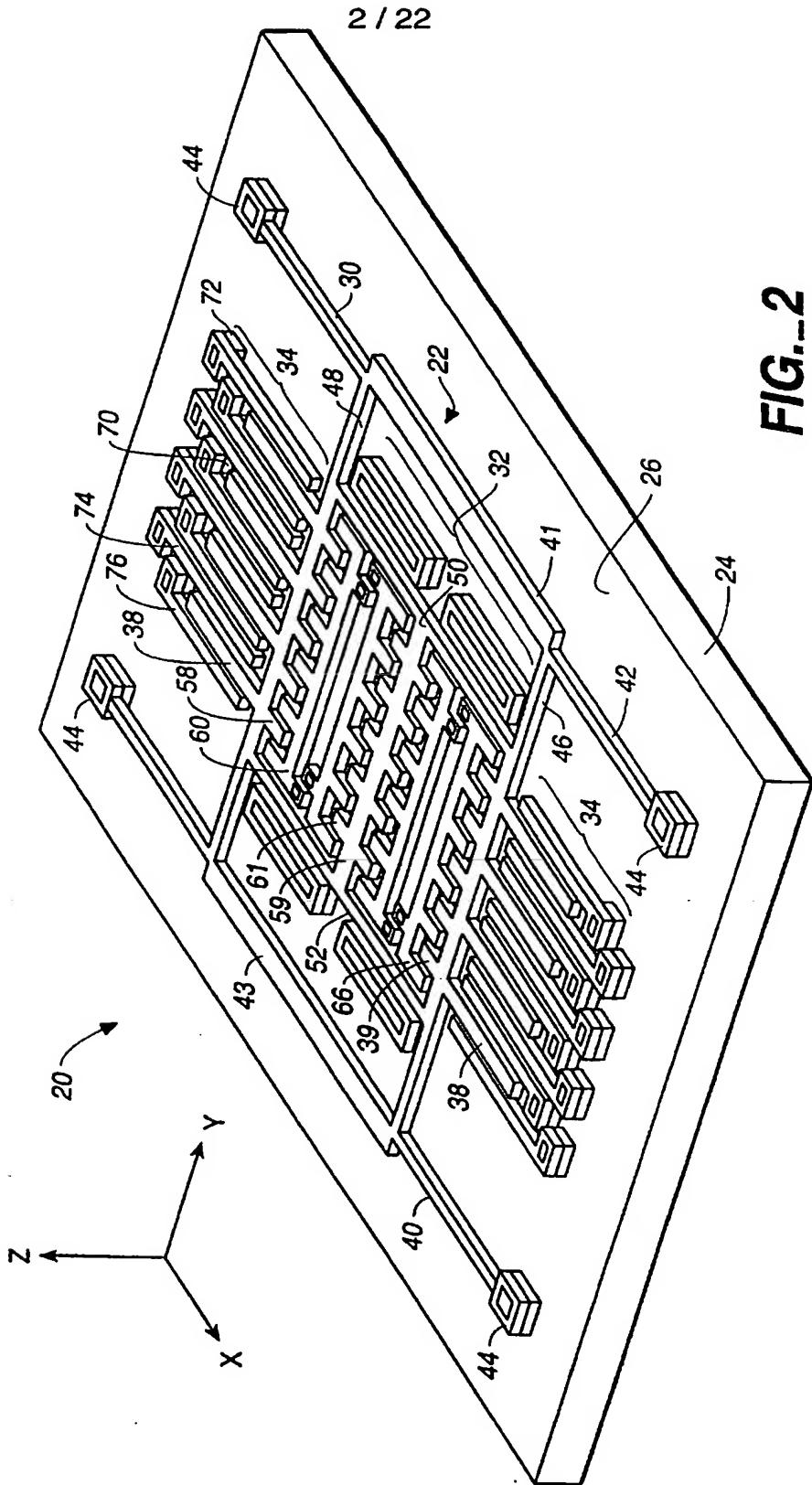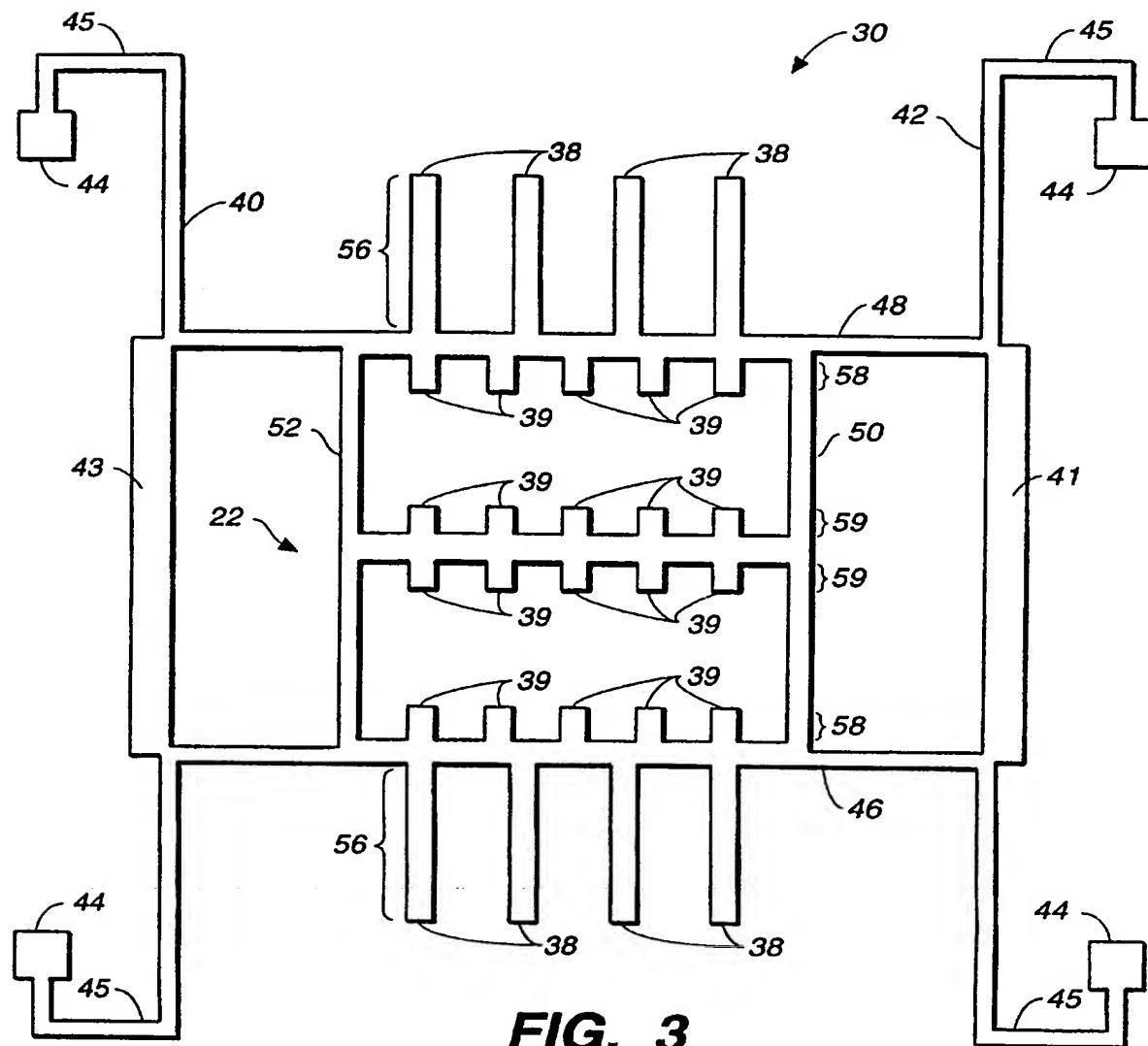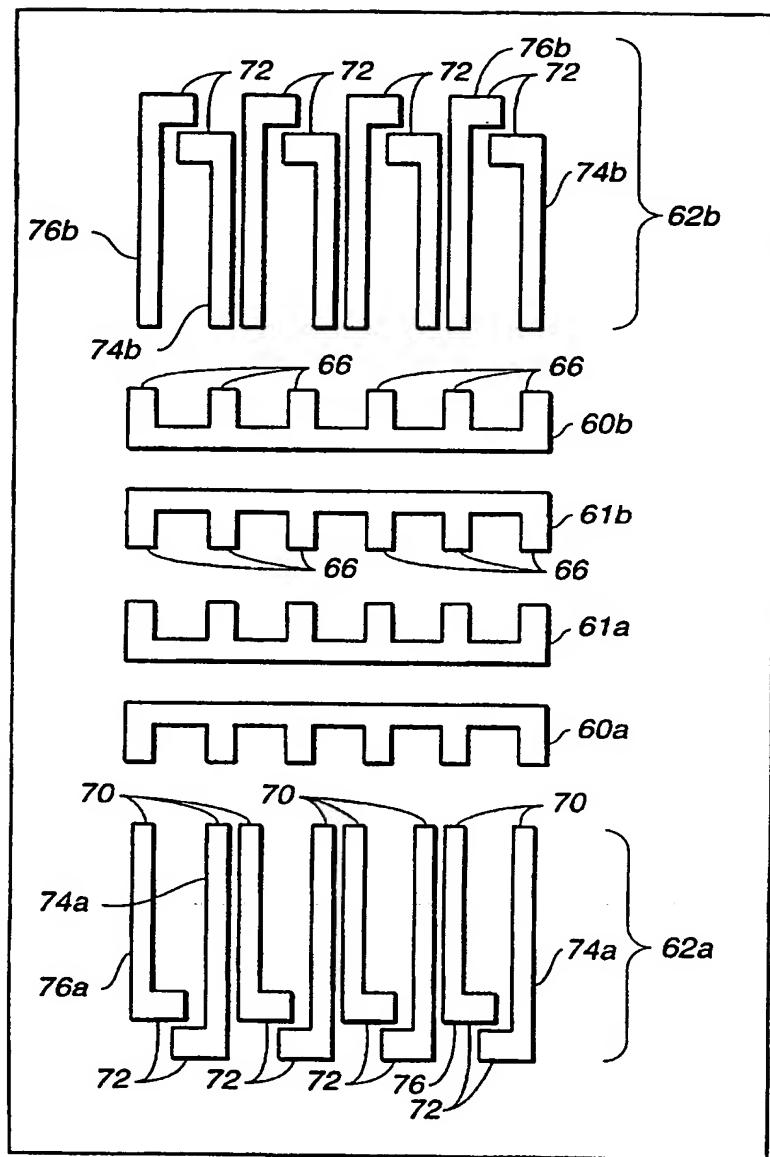
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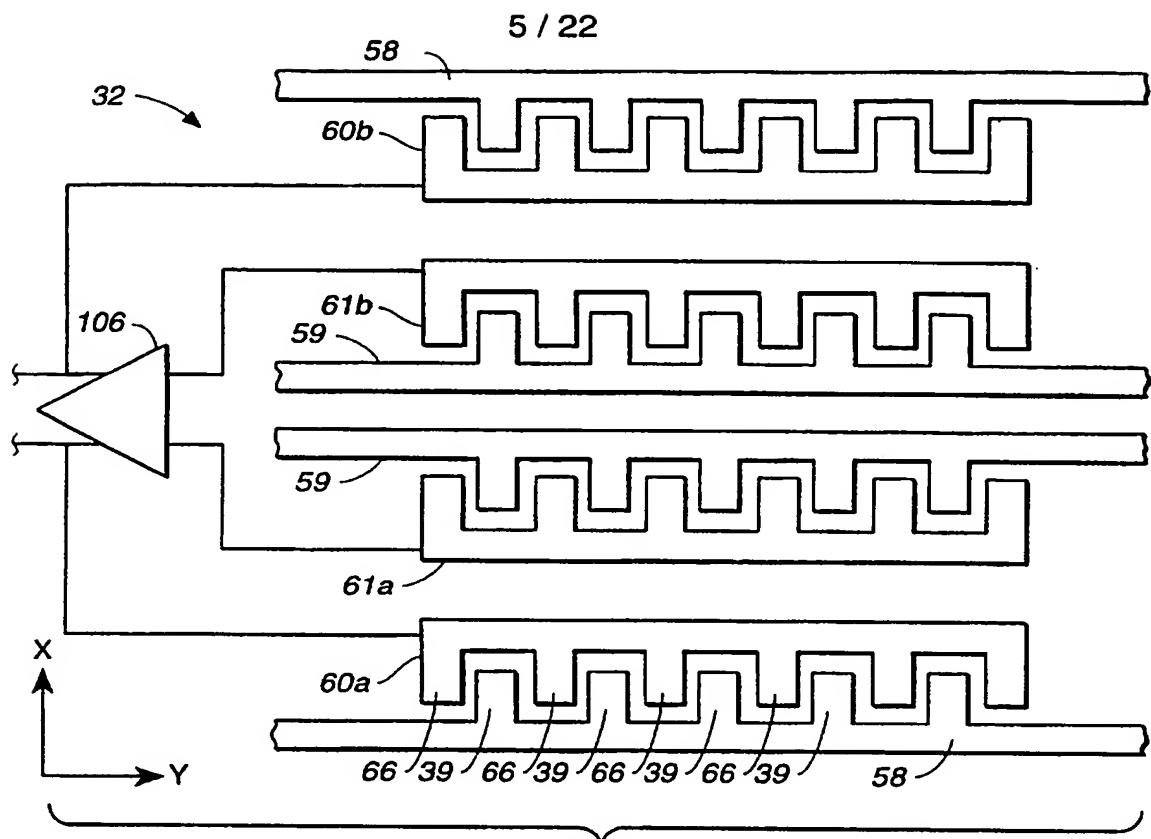
FIG._5

FIG._7A

FIG._7B
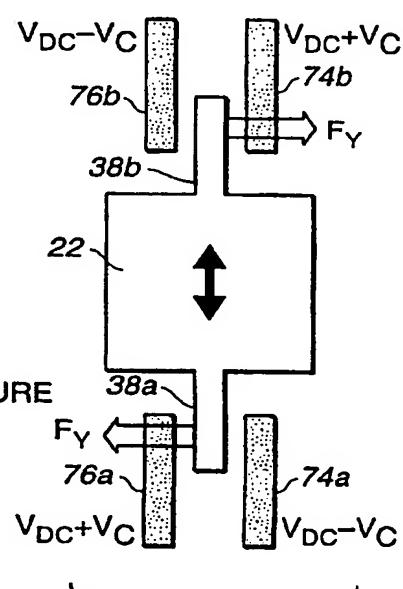
FIG._7C
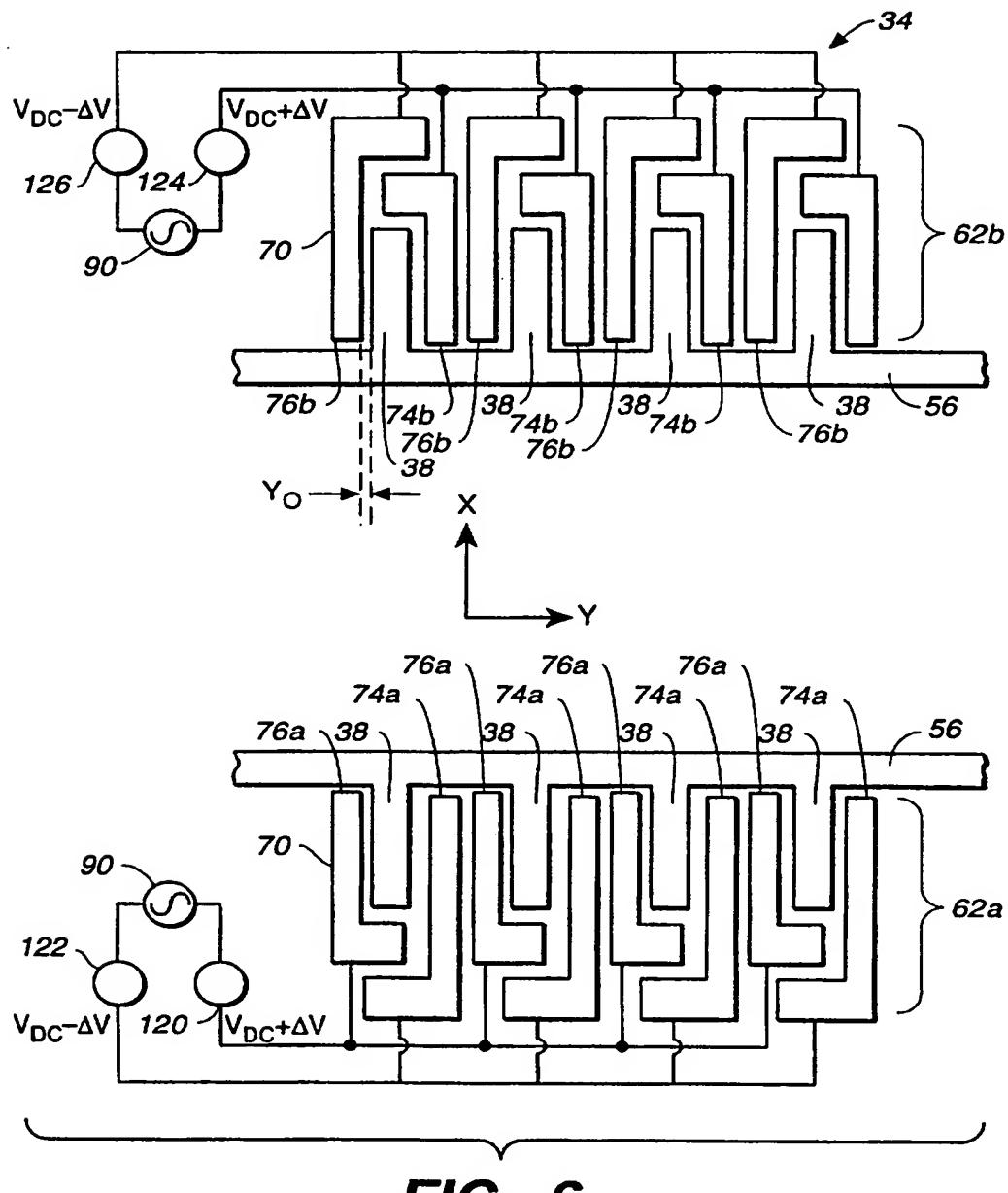
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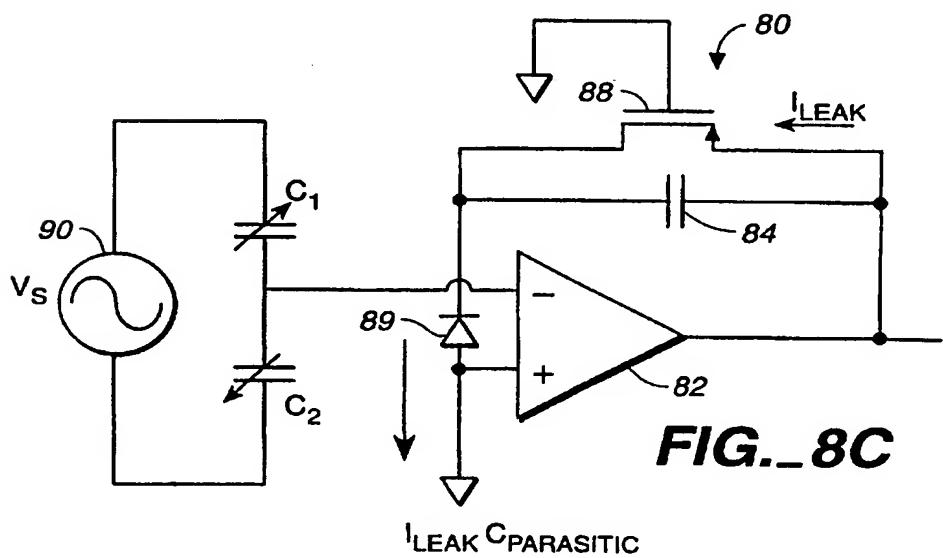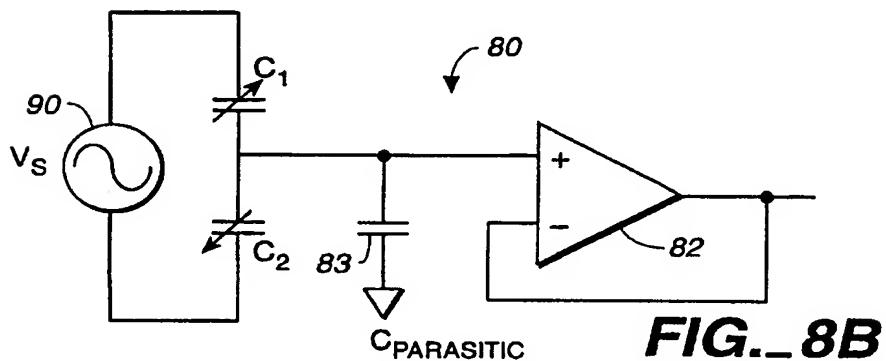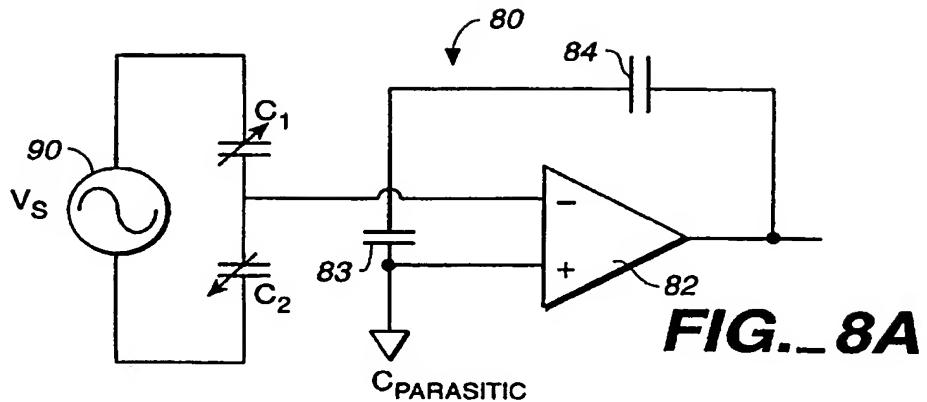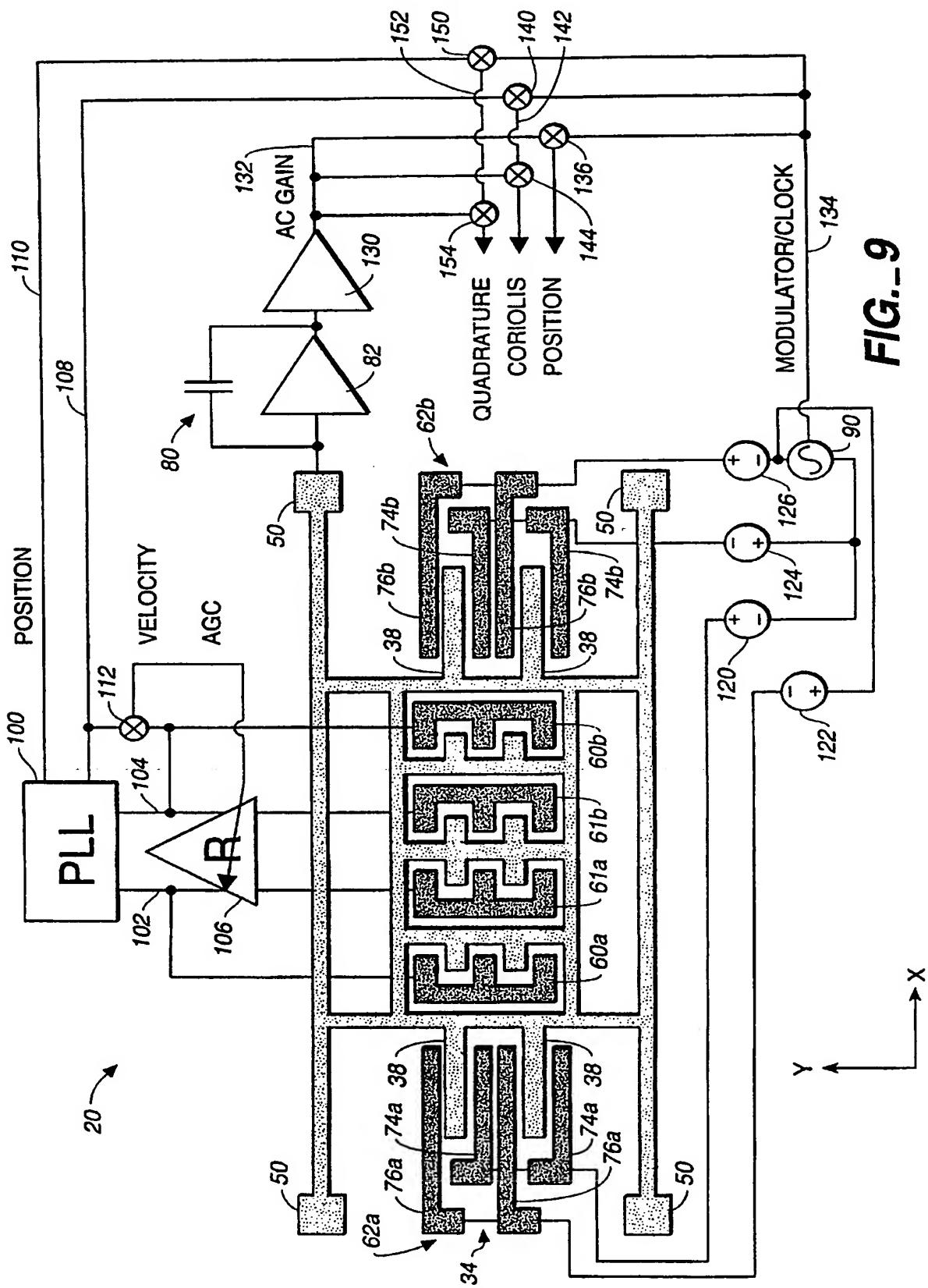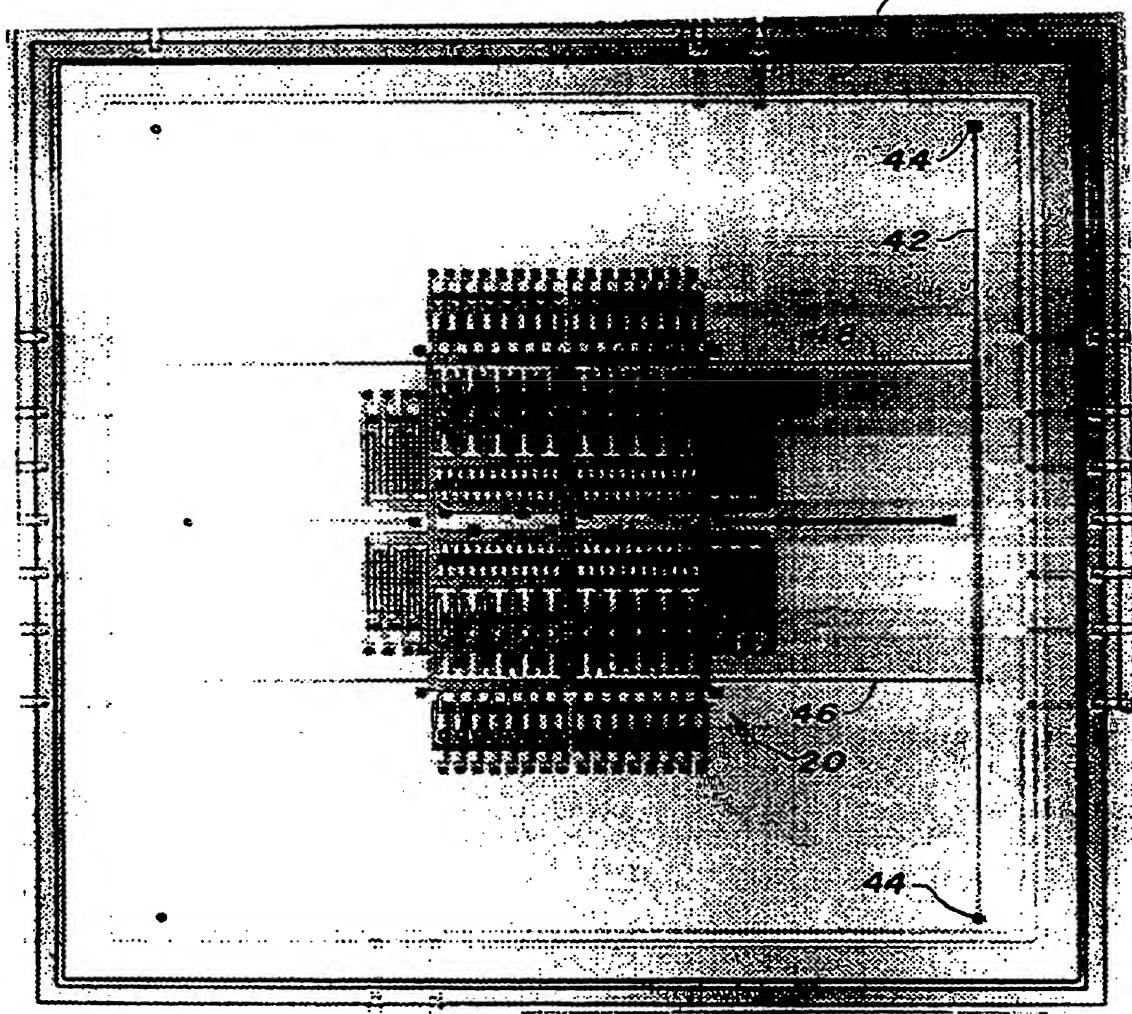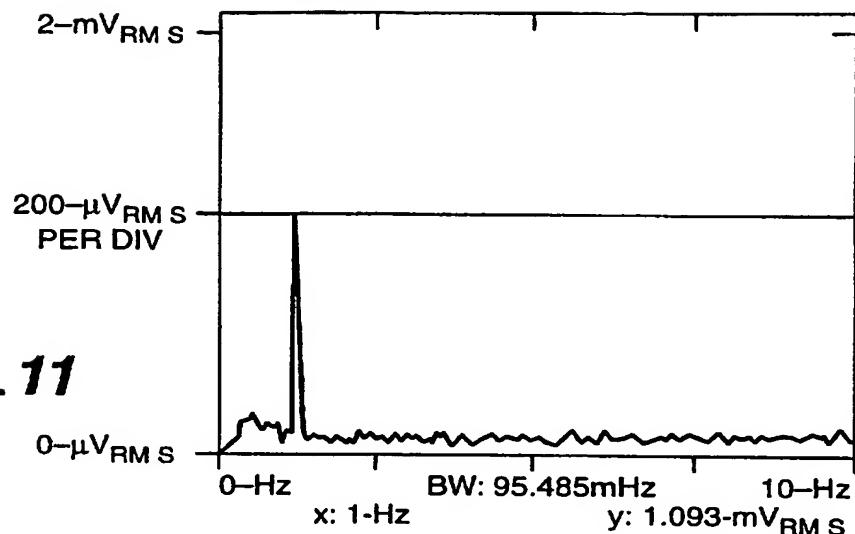
FIG._8A

FIG._8B

FIG._8C

FIG._9

FIG._10

FIG._11

FIG._12

FIG._13

FIG._14

FIG._15

FIG._16

Ω_r 290

ω_z

F_D F_C

F_C F_D

294

292

296

ω_x

Z

Y

X

FIG._19

F_z

392

+ − +

392

344

398

−

306

FIG._17A

FIG._17B

FIG._18

FIG._20

FIG._21

FIG.__22

FIG._23
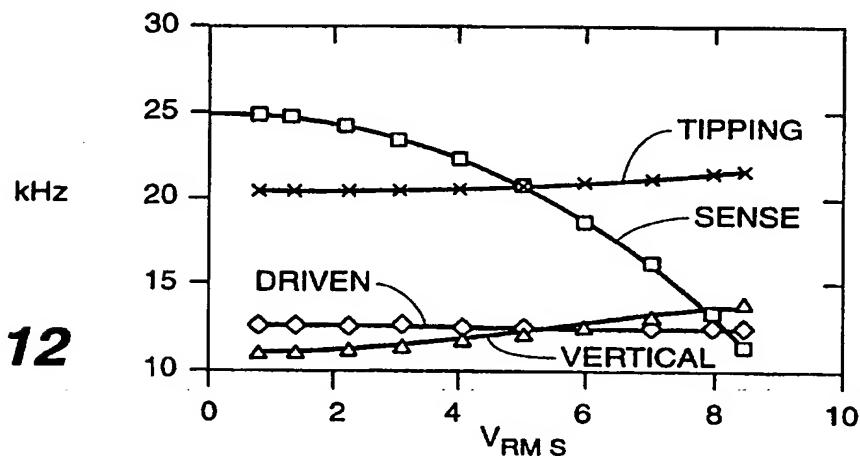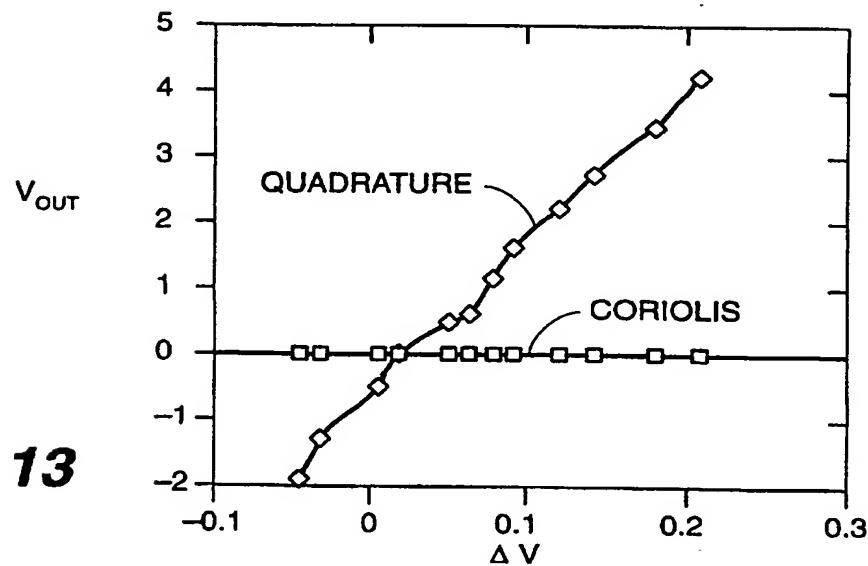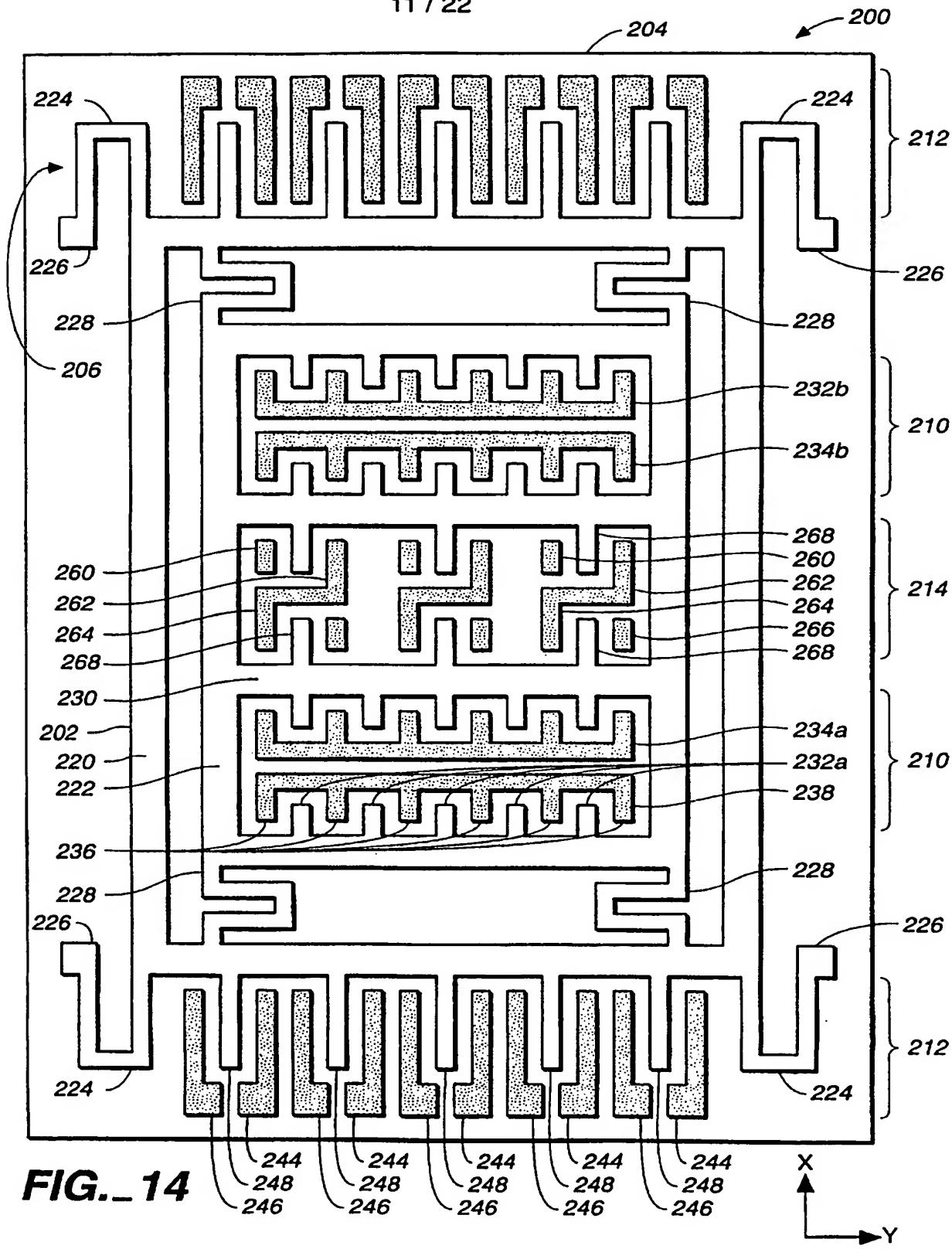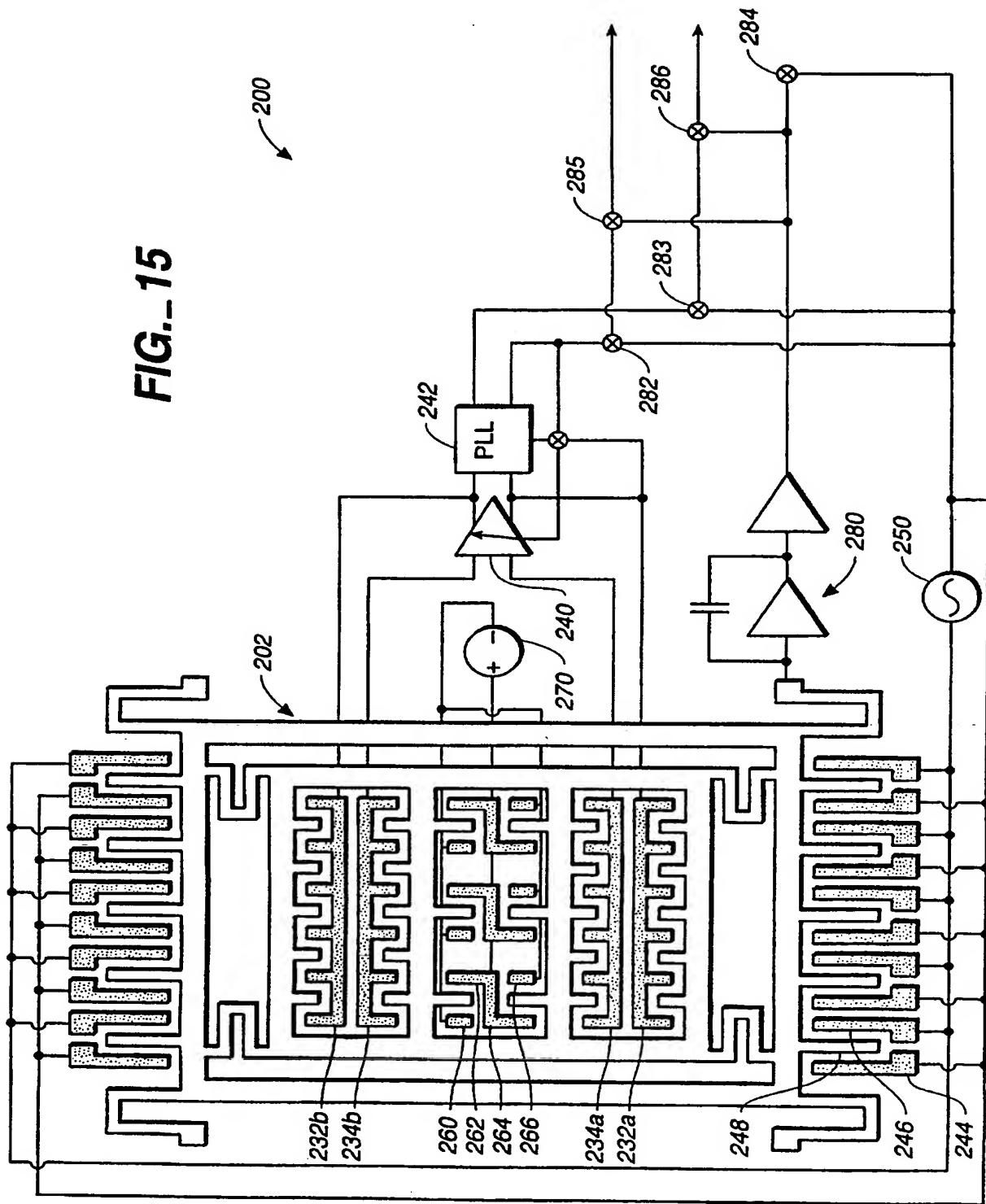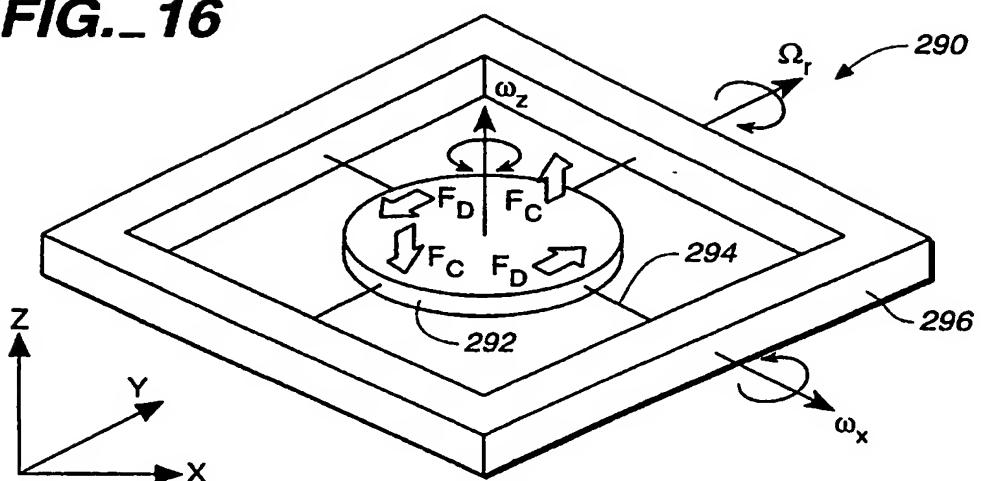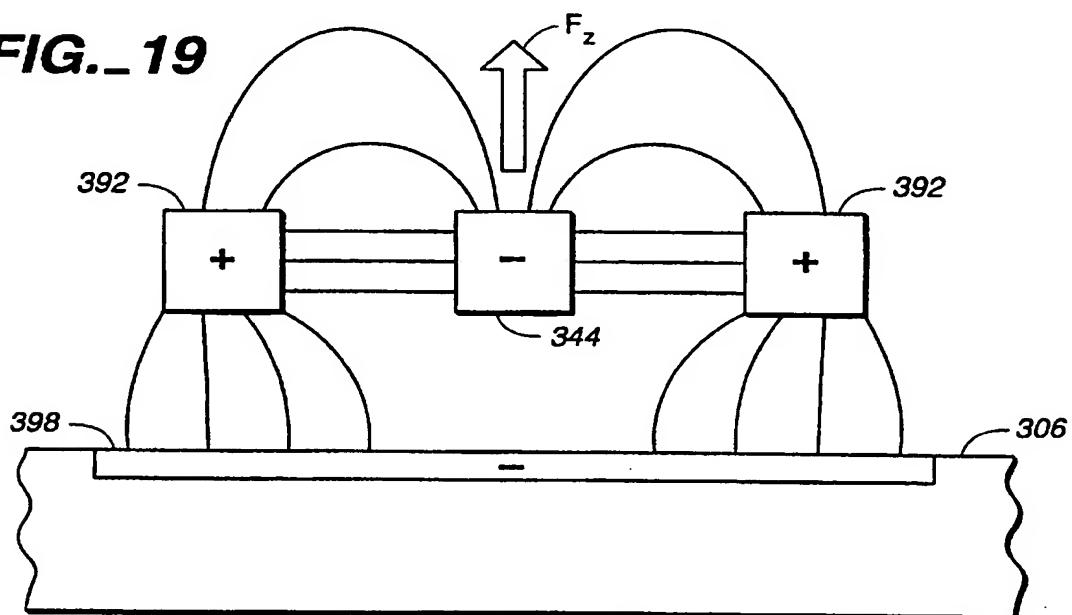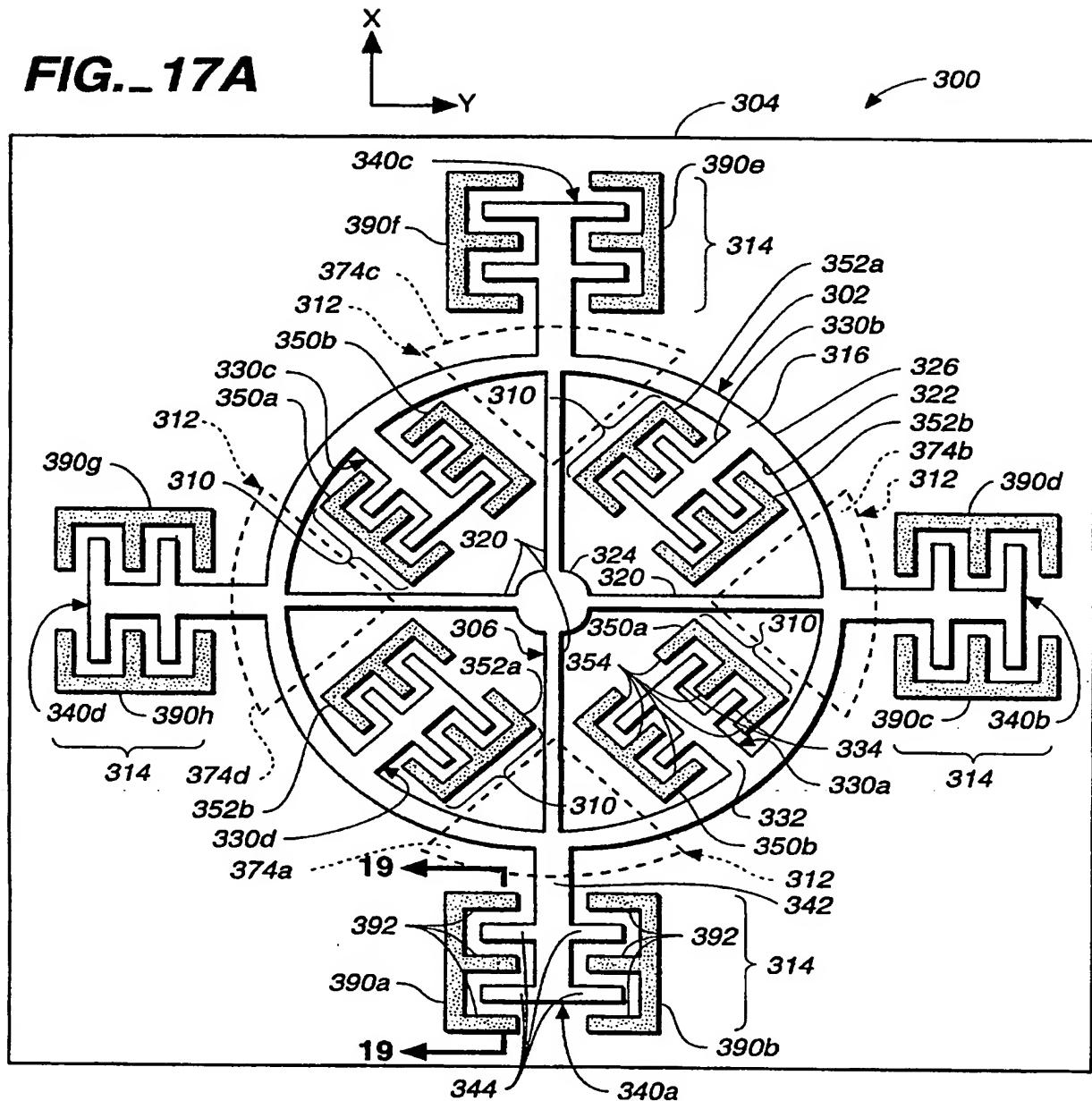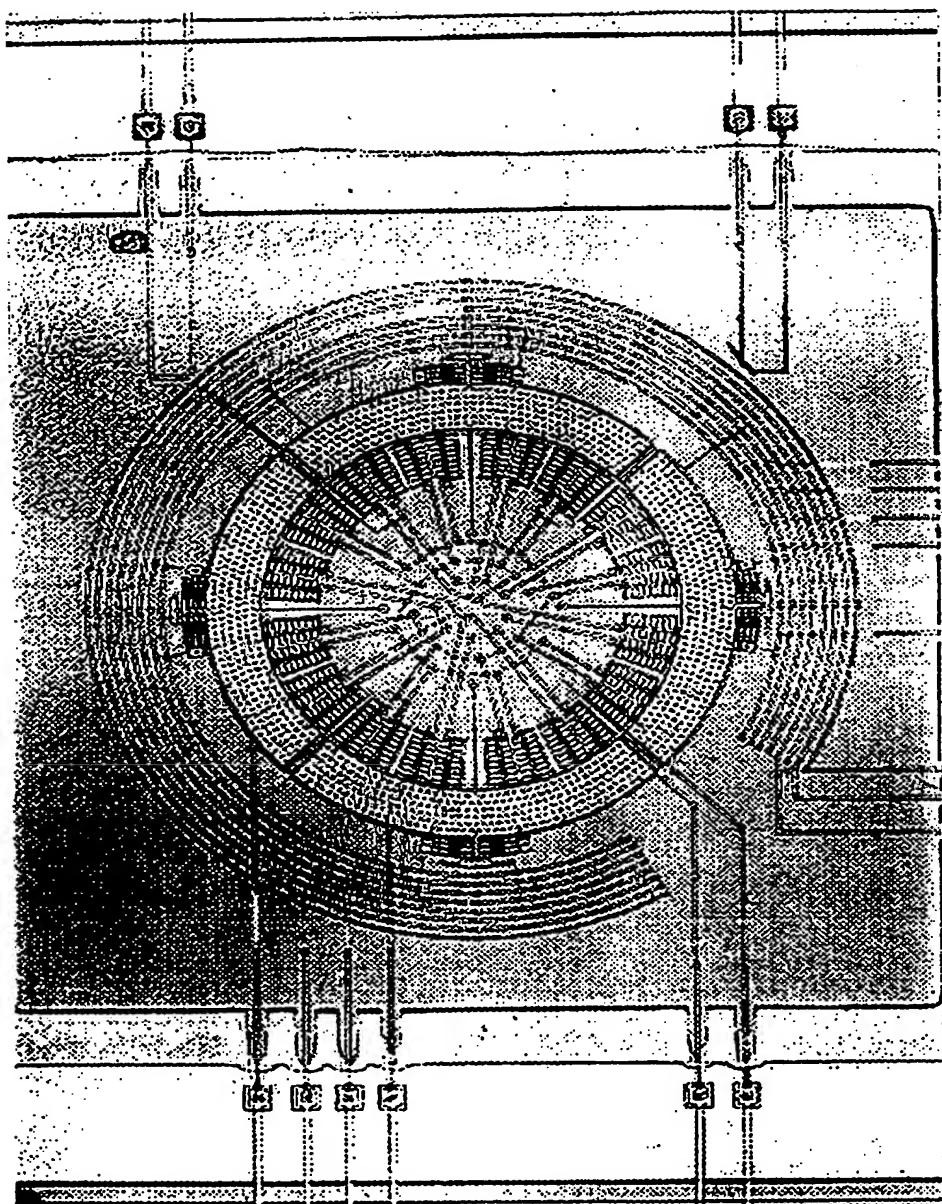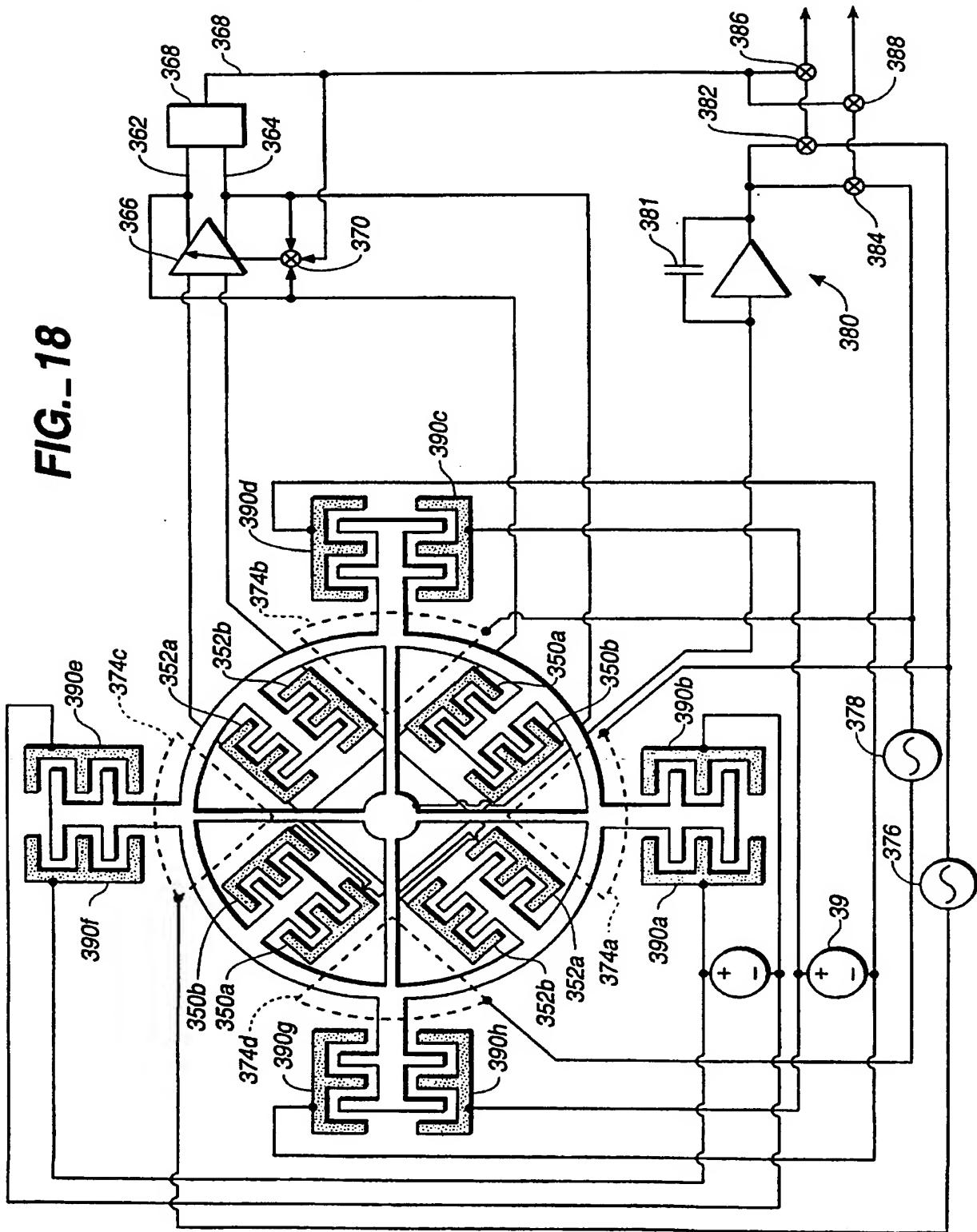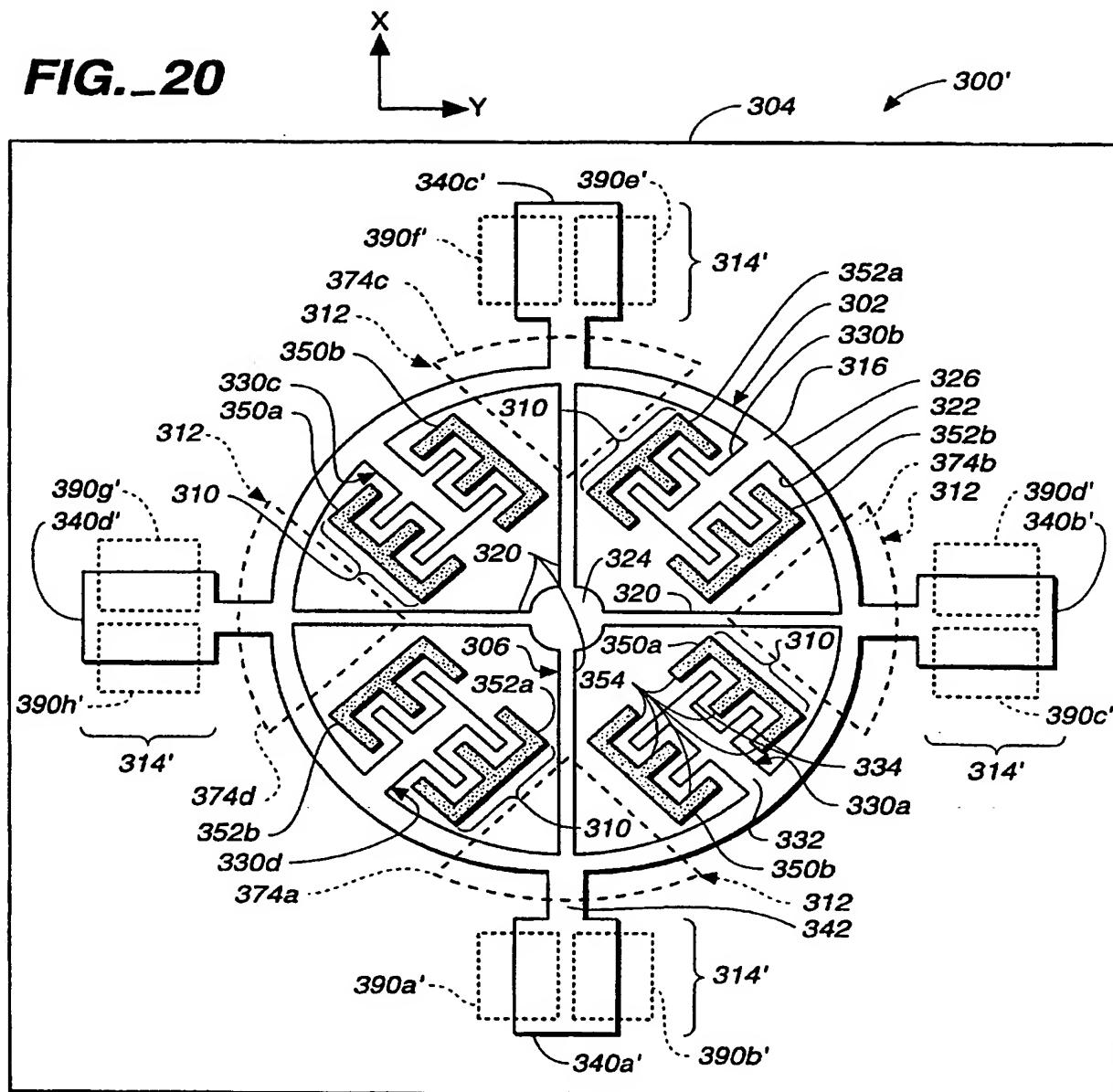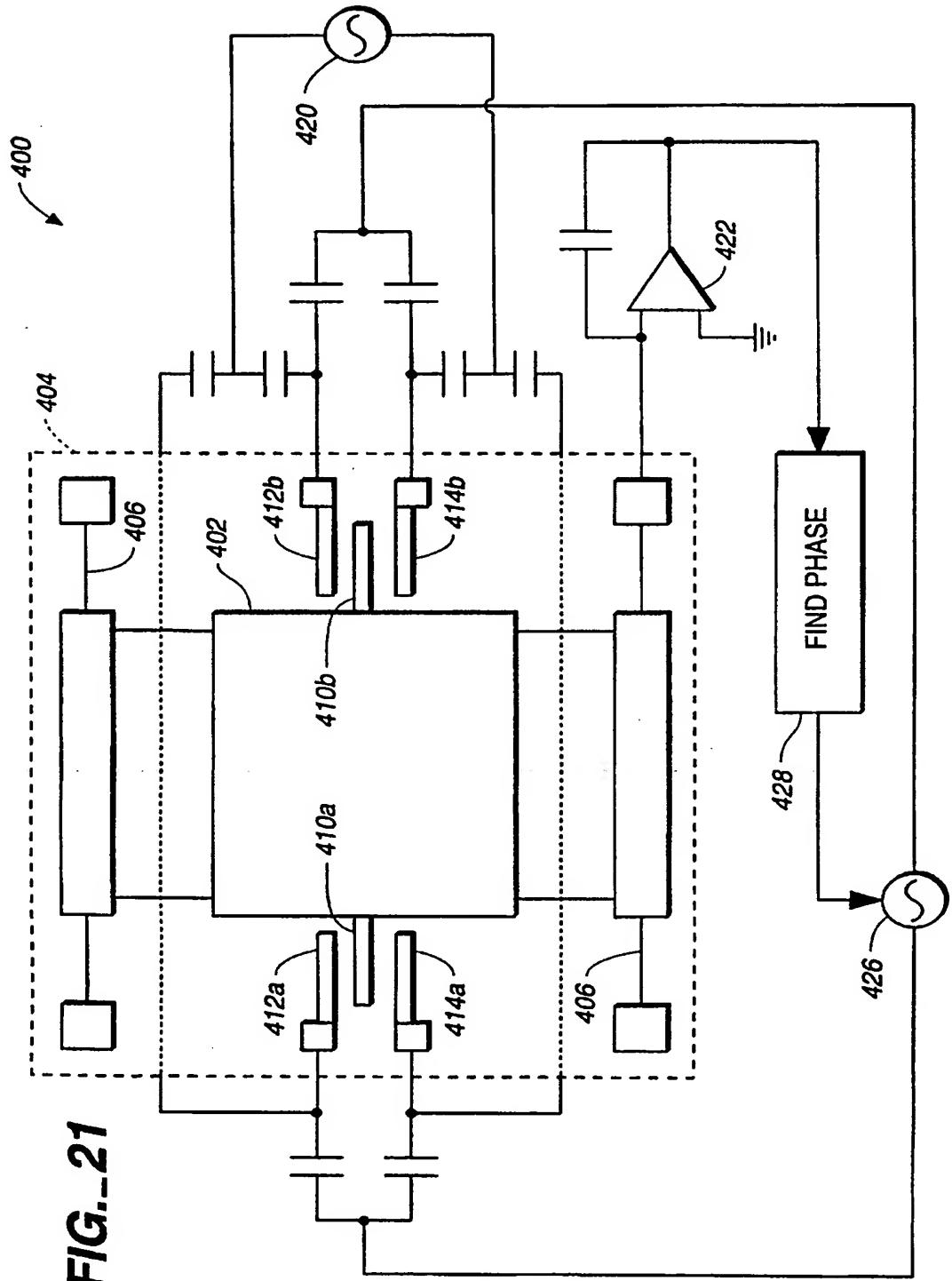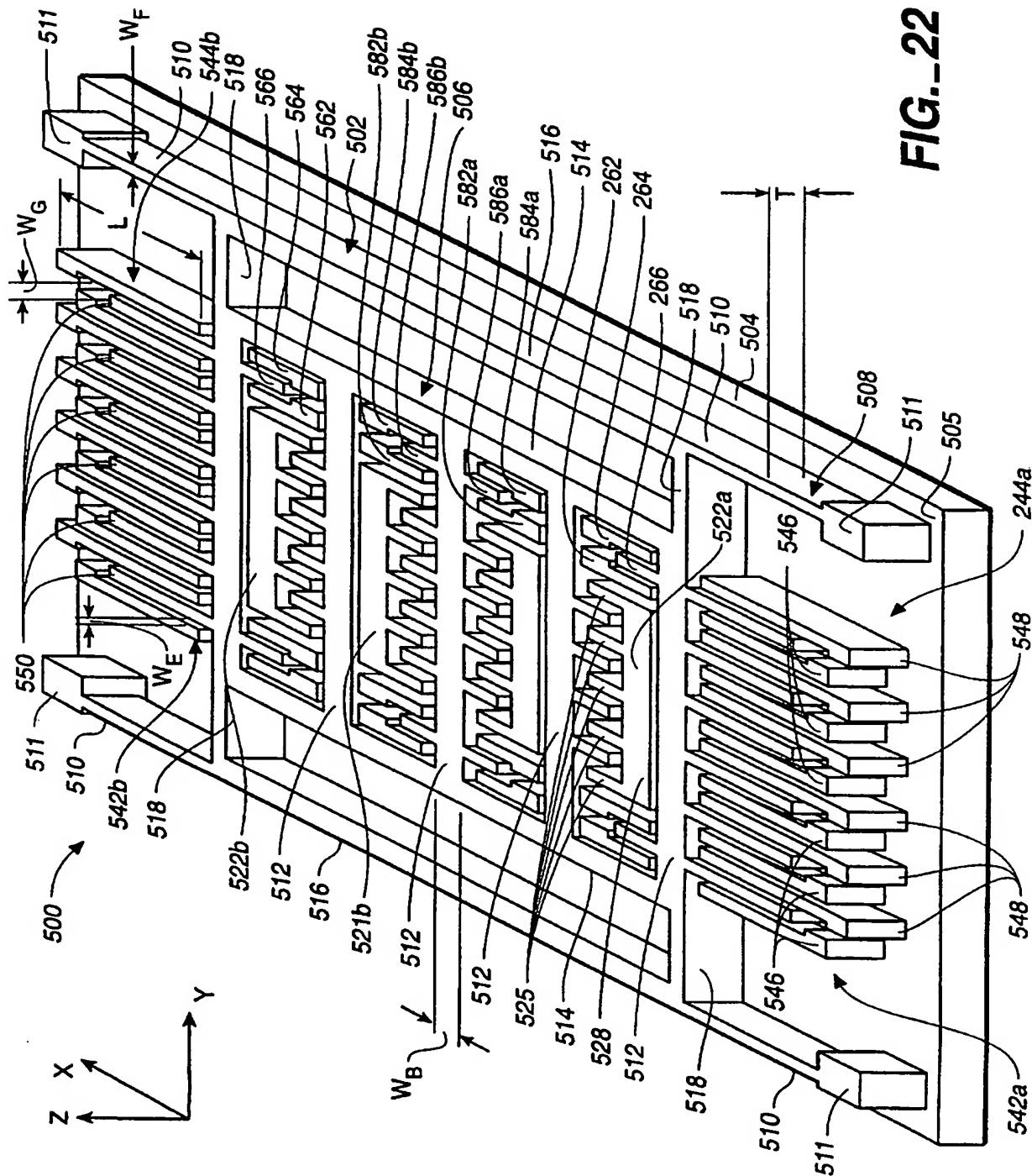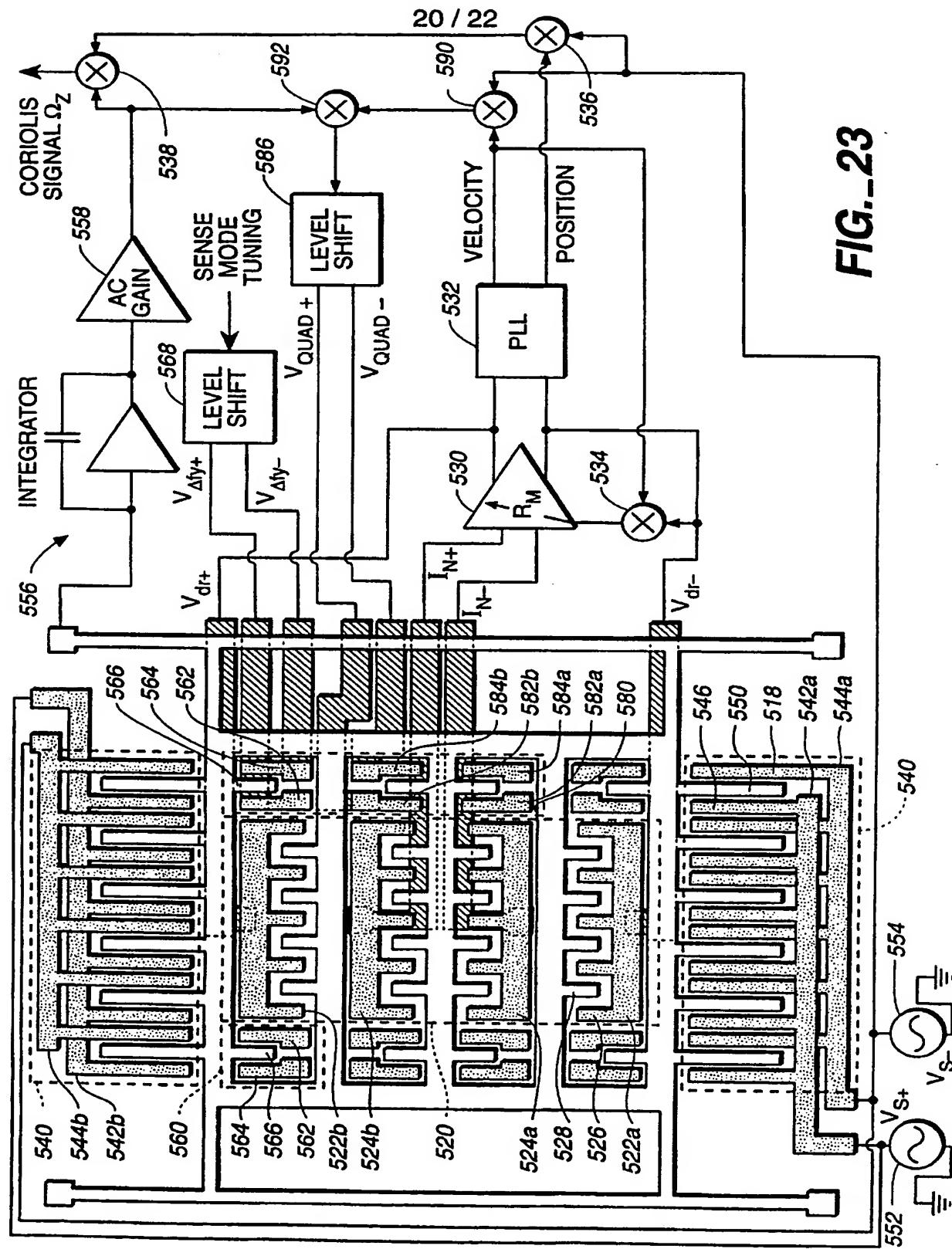
FIG._24A

FIG._24B

FIG._24C

FIG._24D

IC FABRICATION

FIG._24E

FIG._24F

FIG._24G